

**Electrical Engineering Department**  
**Signal Analysis (802321) – G1**

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Start from here →

	الاسم:
	الرقم الجامعي:



Q.1 Choose the correct answer:

*From 1 – 17, 1.5 Each, Total is 25.5*

*From 18 – 45, 1 Each, Total is 28*

*Total Grade is 53.5*

	The unit of the quantity $\omega t$ is:	
1.	a) Rad . s <sup>-1</sup>	b) Hz . s <sup>-1</sup>
	<b>c) Rad</b>	d) Hz . s
	A signal is a power signal if:	
2.	a) $0 < \int_{-\infty}^{\infty}  g(t) ^2 dt < \infty$	b) $0 \leq \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2}  g(t) ^2 dt < \infty$
	c) $\lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2}  g(t) ^2 dt < \infty$	<b>d) <math>0 &lt; \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2}  g(t) ^2 dt &lt; \infty</math></b>
	Calculating the power of any sinusoidal signal depends on:	
3.	a) The phase angle and frequency.	b) The maximum amplitude and phase angle.
	<b>c) The maximum amplitude only.</b>	d) The maximum amplitude and frequency.
	Given the signal $x(t) = C_1 \cos \omega_1 t + C_2 \cos \omega_2 t + C_3 \cos \omega_3 t$ . The power of $x(t)$ is calculated as:	
4.	<b>a) <math>\frac{1}{2} [C_1^2 + C_2^2 + C_3^2]</math></b>	b) $\frac{1}{2} [C_1 + C_2 + C_3]$
	c) $\frac{1}{2} [C_1 + C_2 + C_3]^2$	d) $[C_1^2 + C_2^2 + C_3^2]$
	If a signal is time-shifted, scaled and inverted, which order can be followed?	
5.	a) Scaling → shifting → inversion.	<b>b) Shifting → inversion → scaling.</b>
	c) Inversion → shifting → scaling.	d) All the above.
	Discrete-time signal is a signal that is:	
6.	a) Specified for all values of amplitude.	b) Specified for all values of time.
	c) Specified for some values of amplitude.	<b>d) Specified for some values of time.</b>
	The energy and power of the periodic complex exponential signal $e^{j\omega_0 t}$ are:	
7.	<b>a) Energy is <math>\infty</math>, power is 1.</b>	b) Energy is $\infty$ , power is $T_0$ .
	c) Energy is $T_0$ , power is 1.	d) Energy is $\omega_0$ , power is 1.
	The frequencies of a set of harmonically-related complex exponential signals, with the fundamental frequency $100\pi$ (rad/s), can be:	
8.	a) $100\pi, 150\pi, 350\pi,$ and $550\pi$ .	b) $100\pi, 150\pi, 200\pi,$ and $250\pi$ .
	<b>c) <math>100\pi, 300\pi, 500\pi,</math> and <math>700\pi</math>.</b>	d) $100\pi, 50\pi, 200\pi,$ and $300\pi$ .

	Which one of the following signals is complex?	
9.	a) $ 7e^{-j5000\pi t} $	b) $j^2 \left(\frac{1}{j}t + jt^2\right)$
	c) $\frac{1}{j^2} [e^{j50\pi t} - e^{-j50\pi t}]$	d) $\frac{1}{2} [e^{j50\pi t} + e^{-j50\pi t}]$
	In non-memoryless (dynamic) systems, the output at any instant depends on input values at:	
10.	a) The same or past time.	b) The same and (past and / or future) time.
	c) The same time only.	d) The same and past time only.
	Which one of the following systems is nonlinear:	
11.	a) $y[n] = n x[n]$	b) $y(t) = \frac{1}{2} x(t)$
	c) $y(t) = 2 x(t) + 1.5$	d) $y(t) = 2 t x(t)$
	Fourier series is expressed using the formula $x(t) = a_0 + 2 \sum_{k=1}^{\infty} \frac{a_{-k}}{j} \sin k\omega_0 t$ , when:	
12.	a) $x(t)$ is complex but $\{a_k\}$ are imaginary	b) $x(t)$ is real but $\{a_k\}$ are complex
	c) $x(t)$ is real but $\{a_k\}$ are imaginary	d) $x(t)$ is complex but $\{a_k\}$ are real
	Given a square wave with the following characteristics: $x(t) = \begin{cases} 1 & , \quad  t  \leq 1 \\ 0 & , \quad 1 \leq  t  \leq 2 \end{cases}$	
13.	a) $T_1 = 1, T = 2$	b) $T_1 = \frac{1}{2}, T = 2$
	c) $T_1 = 1, T = 4$	d) $T_1 = \frac{1}{2}, T = 4$
	Given that the signal $x(t)$ in Q.13 has the Fourier series coefficients $a_k$ , if $x(t)$ is time-expanded by 2, then the new Fourier series coefficients $d_k$ will be:	
14.	a) $d_k = a_k$ , and $\omega_0$ is divided by 2	b) $d_k = a_k$ , but $\omega_0$ is doubled
	c) $d_k = a_k / 2$ , but $\omega_0$ remains the same	d) $d_k = a_k / 2$ , and $\omega_0$ is doubled
	The Fourier transform of the signal $x(t) = e^{3t} u(-t)$ is:	
15.	a) $X(j\omega) = \frac{1}{3+j\omega}$	b) $X(j\omega) = \frac{1}{3-j\omega}$
	c) $X(j\omega) = \frac{6}{9+\omega^2}$	d) $X(j\omega) = \frac{3}{9+\omega^2}$
	Which function can be the Fourier transform of a periodic signal $x(t)$ ?	
16.	a) $X(j\omega) = \frac{1}{2} \sum_{k=-\infty}^{\infty} \delta(\omega - k\omega_0)$	b) $X(j\omega) = \frac{1}{2} \sum_{k=-\infty}^{\infty} \text{sinc}(\omega - k\omega_0)$
	c) $X(j\omega) = \frac{1}{2} \sum_{k=-\infty}^{\infty} u(\omega - k\omega_0)$	d) $X(j\omega) = \sum_{k=-\infty}^{\infty} \frac{\sin k\omega_0}{k} \delta(\omega - \omega_0)$
	Inverse Fourier transform is calculated as:	
17.	a) $x(t) = \int_{-\infty}^{\infty} X(f) e^{j2\pi ft} df$	b) $x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(f) e^{j2\pi ft} df$
	c) $x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) e^{-j\omega t} d\omega$	d) $x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) e^{j\omega t} dt$

18.	Which one of the following signals has both even and odd parts (that are not equal to zero)?	
	a) $\cot \omega_0 t$	b) $t^{-2}$
	c) $\sin \omega_0 t$	d) $e^{2t}$
19.	The noise signal is classified as:	
	a) Power and random signal.	b) Energy and random signal.
	c) Power and deterministic signal.	d) Energy and deterministic signal.
20.	Given an exponential signal $x(t)$ . If the exponent equals $j2000\pi t$ , the fundamental frequency and period-energy equal:	
	a) $f_0 = 1000$ Hz, $E_{x \text{ period}} = \infty$ .	b) $f_0 = 2000\pi$ Hz, $E_{x \text{ period}} = \infty$ .
	c) $f_0 = 1000$ Hz, $E_{x \text{ period}} = 1$ m.	d) $f_0 = 2000\pi$ Hz, $E_{x \text{ period}} = 1$ m.
21.	Which statement is correct?	
	a) $\delta(t)$ is undefined at $t = 0$	b) $\delta[n]$ is undefined at $n = 0$
	c) $\delta(t) = 1$ at $t = 0$	d) $\delta[n] = 1$ for all real values of $n$
22.	The <u>running sum</u> of the function $x[n]$ is:	
	a) $\sum_{m=-\infty}^n x[m]$	b) $\sum_{m=0}^n x[m]$
	c) $\sum_{m=-\infty}^{\infty} x[m]$	d) $\sum_{m=1}^{\infty} x[m]$
23.	Which one of the following systems is <u>causal</u> ?	
	a) $x(t) = \sum_{n=-\infty}^0 x(n)$	b) $x(t) = \sum_{n=-\infty}^{t+1} x(n)$
	c) $x(t) = \sum_{n=t}^{\infty} x(n)$	d) $x(t) = \sum_{n=-\infty}^t x(n)$
24.	The system $y(t) = x(4 - 2t)$ is:	
	a) Nonlinear and time-invariant	b) Linear and time-invariant
	c) Nonlinear and time-variant	d) Linear and time-variant
25.	For the periodic signal: $x(t) = \cos\left(\frac{\pi}{t}\right)$ for $0 < t \leq 2$ :	
	a) $\omega_0 = \pi$ , and $\{a_k\}$ are invalid.	b) $\omega_0 = \pi$ , and $\{a_k\}$ are valid.
	c) $\omega_0 = \frac{\pi}{t^2}$ , and $\{a_k\}$ are invalid.	d) $\omega_0 = \frac{\pi}{t}$ , and $\{a_k\}$ are invalid.
26.	Given the signal: $x(t) = 1 + \cos \frac{16\pi}{3} t + \frac{1}{2} \cos 4\pi t - \sin \frac{4\pi}{3} t$ . The fundamental period of $x(t)$ is:	
	a) $T = 0.5$	b) $T = 0.4$
	c) $T = 1.5$	d) None of the above.

	In the signal $x(t)$ given in Q.26, the harmonics which exist are:	
27.	a) 1 <sup>st</sup> , 2 <sup>nd</sup> and 3 <sup>rd</sup> .	b) 1 <sup>st</sup> , 2 <sup>nd</sup> and 4 <sup>th</sup> .
	c) 2 <sup>nd</sup> , 3 <sup>rd</sup> and 4 <sup>th</sup> .	d) 1 <sup>st</sup> , 3 <sup>rd</sup> and 4 <sup>th</sup> .
28.	A periodic signal is given by: $x(t) = 2 + \cos\left(\frac{4\pi}{3}t\right) + \frac{1}{2}\cos\left(\frac{10\pi}{3}t\right)$	
	The fundamental frequency of $x(t)$ is:	
	a) $\omega_0 = 4\pi/3$	b) $\omega_0 = 2\pi/3$
	c) $\omega_0 = \pi/3$	d) $\omega_0 = 3\pi/2$
29.	The Fourier series coefficients $a_k$ of the signal $x(t)$ given in Q.28 are:	
	a) $a_0 = 2, a_2 = a_{-2} = 0.5, a_5 = a_{-5} = 0.25$	b) $a_0 = 2, a_1 = a_{-1} = 0.5, a_5 = a_{-5} = 0.25$
	c) $a_0 = 2, a_2 = a_{-2} = 1, a_5 = a_{-5} = 0.5$	d) $a_0 = 2, a_2 = a_{-2} = 0.5, a_{10} = a_{-10} = 0.25$
30.	Fourier series can be used to represent:	
	a) All periodic signals.	b) Almost all periodic signals.
	c) Large set of periodic signals.	d) Some periodic signals.
31.	Given the signal $x(t) = \cos^2 3\pi t$ . If the fundamental frequency in radian per second is $3\pi$ :	
	a) $a_0 = 1/2, a_1 = 0, a_2 = 1/2$	b) $a_0 = 1/2, a_1 = 1/4, a_2 = 0$
	c) $a_0 = 0, a_1 = 1/4, a_2 = 0$	d) $a_0 = 1/2, a_1 = 0, a_2 = 1/4$
32.	For the signal $x(t)$ given in Q.13 (the square wave):	
	a) $a_0 = 1/2, a_k = (1/k\pi) \sin(k\pi/2)$ for $k \neq 0$	b) $a_0 = 1, a_k = (1/k\pi) \sin(k\pi/2)$ for $k \neq 0$
	c) $a_0 = 1/2, a_k = (1/k\pi) \sin(k\pi)$ for $k \neq 0$	d) $a_0 = 1, a_k = (1/k\pi) \sin(k\pi)$ for $k \neq 0$
33.	If the signal $x(t)$ given in Q.13 is shifted up by $1/4$ , then the new Fourier series coefficients $b_k$ will be:	
	a) $b_k = a_k + 1/4$ , for $k = 0$	b) $b_k = a_k + 1/4$ , for all values of $k$
	c) $b_k = a_k$ but frequency is shifted by $1/4$	d) $b_k = a_k - 1/4$ , for $k = 0$
34.	If the signal $x(t)$ given in Q.13 is time-reversed, then the new Fourier series coefficients $c_k$ will be:	
	a) $c_0 = a_0, c_k = a_{-k} = -a_k$	b) $c_0 = a_0, c_k = a_{-k} = a_k$
	c) $c_0 = -a_0, c_k = a_{-k} = a_k$	d) $c_0 = -a_0, c_k = a_{-k} \neq -a_k$
35.	If the signal $x(t)$ given in Q.13 is shifted to the left by $1/2$ , then the new Fourier series coefficients $e_k$ will be:	
	a) $e_0 = a_0, e_k = a_k e^{-jk(\pi/4)}$ for $k \neq 0$	b) $e_0 = a_0, e_k = a_k e^{-jk(\pi/2)}$ for $k \neq 0$
	c) $e_0 = a_0, e_k = a_k e^{jk(\pi/4)}$ for $k \neq 0$	d) $e_0 = 0, e_k = a_k e^{-jk(\pi/4)}$ for $k \neq 0$
36.	If $a_k$ are the Fourier series coefficients of a signal $g(t)$ , the Fourier series coefficients of the signal $dx(t)/dt$ are:	
	a) $(1/jk\omega_0) a_k$	b) $jk\omega_0 a_k$
	c) $(-1/jk\omega_0) a_k$	d) $-jk\omega_0 a_k$

	For which signal do we have to sketch the magnitude and phase of its Fourier transform?	
37.	a) $x(t) = e^{-12 t }$	b) $x(t) = 5 \text{ rect}(2t)$
	c) $x(t) = \cos 200\pi t$	d) $1/3 u(t)$
	The Fourier transform of the signal $x(t) = e^{-at}u(t)$ equals to:	
38.	a) $F\{e^{-a t } - e^{at}u(-t)\}$	b) $F\{e^{-a t }\} - F\{e^{at}u(-t)\}$
	c) $F\{e^{at}u(-t)\} - F\{e^{-a t }\}$	d) $F\{e^{-a t }\} + F\{e^{at}u(-t)\}$
	The function $X(j\omega) = \text{sinc}(3.5\omega)$ is the Fourier transform of the signal:	
39.	a) $x(t) = \frac{1}{7} \text{ rect}\left(\frac{t}{7}\right)$	b) $x(t) = \frac{1}{3.5} \text{ rect}\left(\frac{t}{3.5}\right)$
	c) $x(t) = 7 \text{ rect}\left(\frac{t}{7}\right)$	d) $x(t) = 3.5 \text{ rect}\left(\frac{t}{3.5}\right)$
	The function $X(j\omega) = \pi e^{ \omega }$ is the Fourier transform of the signal:	
40.	a) $x(t) = \frac{2}{1+t^2}$	b) $x(t) = \frac{1}{t^2+1}$
	c) $x(t) = \frac{1}{t^2-1}$	d) None of the above
	Given the energy aperiodic signal $x(t) = t$ , for $-1 \leq t \leq 1$ . If $y(t) = \frac{dx(t)}{dt}$ , then $y(t)$ equals:	
41.	a) $y(t) = \text{rect}\left(\frac{t}{2}\right) - \delta(t+1) + \delta(t-1)$	b) $y(t) = \text{rect}\left(\frac{t}{2}\right) - \delta(t+1) - \delta(t-1)$
	c) $y(t) = \text{rect}\left(\frac{t}{2}\right) + \delta(t+1) + \delta(t-1)$	d) $y(t) = \text{rect}\left(\frac{t}{2}\right)$
	Using the integration property to find the Fourier transform of $x(t)$ in Q.41:	
42.	a) $X(j\omega) = \frac{1}{j\omega} Y(j\omega) + \pi Y(0) \delta(\omega)$	b) $X(j\omega) = \frac{1}{j\omega} Y(j\omega) + \pi X(0) \delta(\omega)$
	c) $X(j\omega) = \frac{1}{j\omega} Y(j\omega)$	d) $X(j\omega) = \frac{1}{j\omega} Y(j\omega) + \pi \delta(\omega)$
	The signum function $\text{sgn}(t)$ can be defined as:	
43.	a) $\text{sgn}(t) = u(t) + u(-t)$	b) $\text{sgn}(t) = 1 - 2u(t)$
	c) $\text{sgn}(t) = u(t) - u(-t)$	d) b) and c)
	The Fourier transform of the function $\text{sgn}(t)$ is:	
44.	a) $1/j\omega$	b) $2/j\omega + 2\pi \delta(\omega) - 1$
	c) $2/j\omega$	d) $2/j\omega - \pi \delta(\omega)$
	What is the Fourier transform of the triangular function $\Delta\left(\frac{t}{\tau}\right)$ . Note that this is a single triangular pulse with amplitude 1 and width $\tau$ .	
45.	a) $\delta\left(\omega - \frac{2\pi}{\tau}\right)$	b) $\frac{\tau}{2} \text{sinc}\left(\frac{\omega\tau}{4}\right)$
	c) $\Delta\left(\frac{\omega\tau}{2}\right)$	d) $\frac{\tau}{2} \text{sinc}^2\left(\frac{\omega\tau}{4}\right)$