



Data Structures

Chapter 3: Sorting

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Sorting Algorithms

1. Sorting Definition
2. Bubble Sort
3. Selection Sort
4. Insertion Sort

1. Sorting Definition

❑ Motivation

- ❑ Generally, to arrange a list of elements in some order

❑ List of numbers

- 10 20 50 30 40 60 25 (Unsorted list)
- 10 20 25 30 40 50 60 (Sorted list, ascending)
- 60 50 40 30 25 20 10 (Sorted list, descending)

❑ List of alphabets

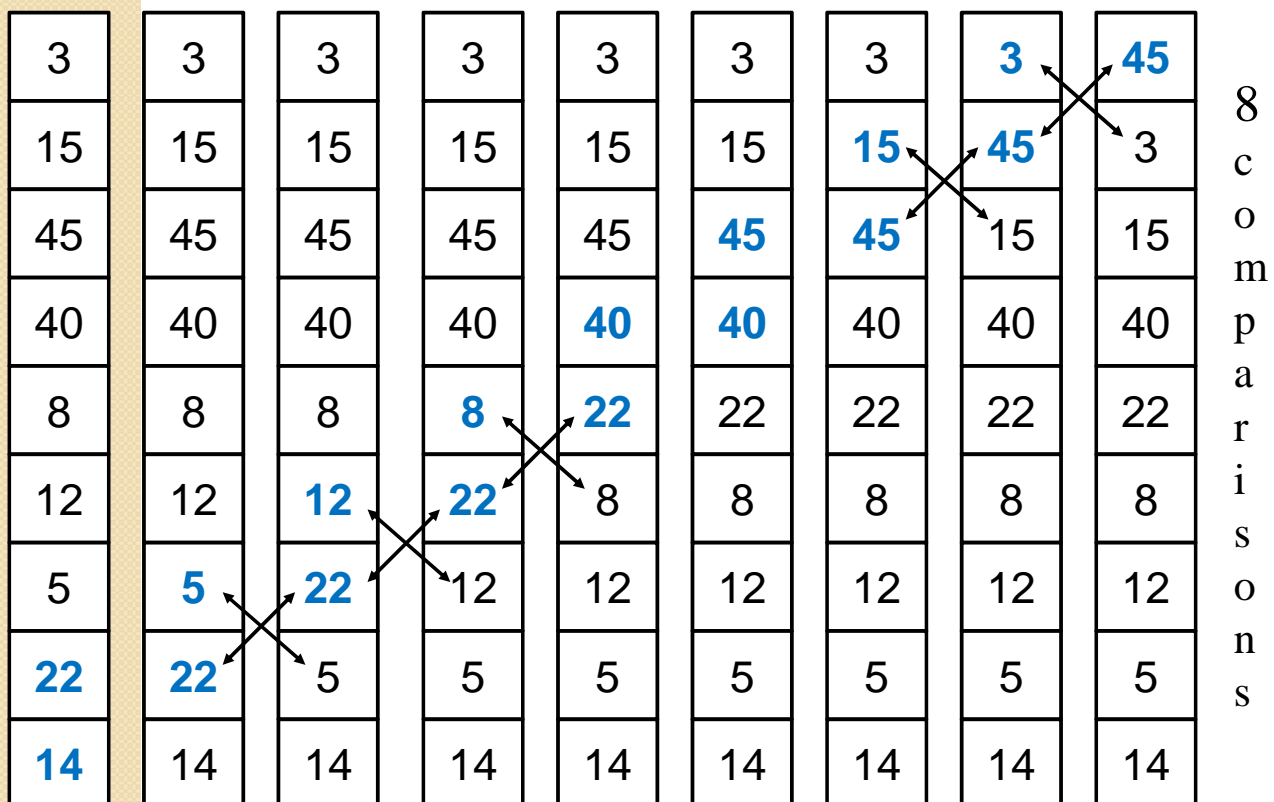
- P A K I S T A N (Unsorted list)
- A A I K N P S T (Sorted list, ascending)
- T S P N K I A A (Sorted list, descending)

2. Bubble Sort

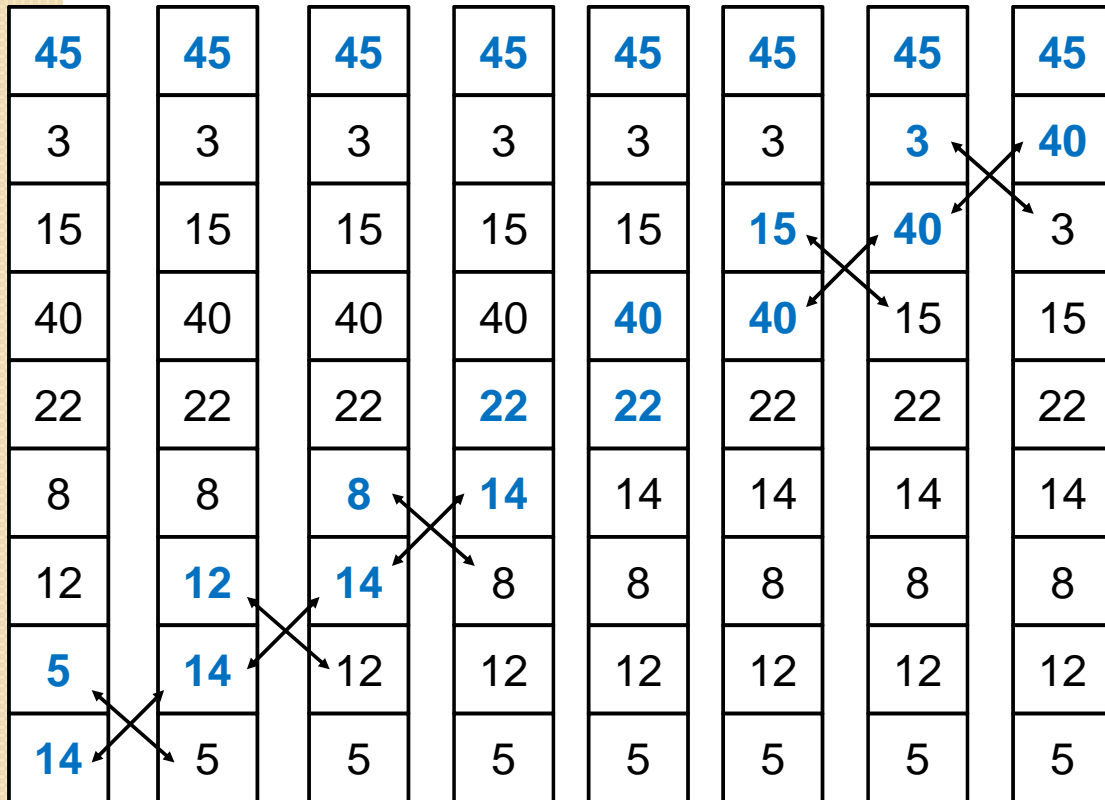
Bubble Sort Algorithm: Informal

- Repeatedly compare the elements at consecutive locations in a given list, and do the following until the elements are in required order:
 - If elements are not in the required order, swap them (change their position)
 - Otherwise do nothing

Bubble Sort in Action: Phase 1

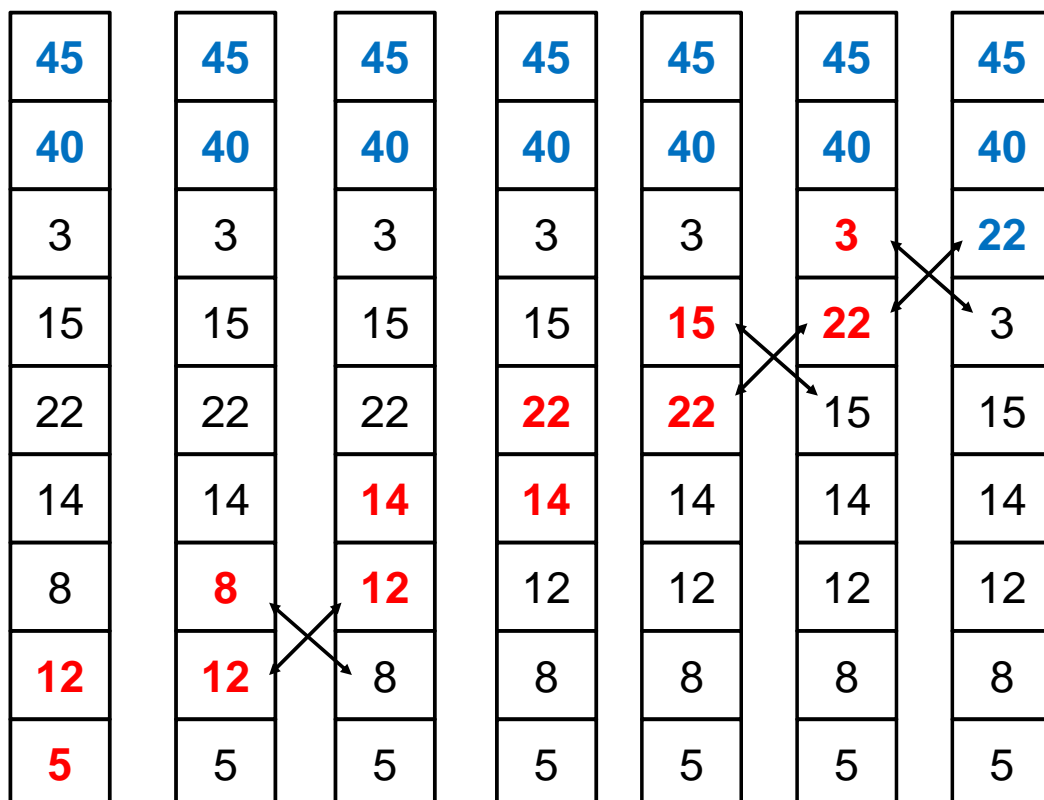


Bubble Sort in Action: Phase 2



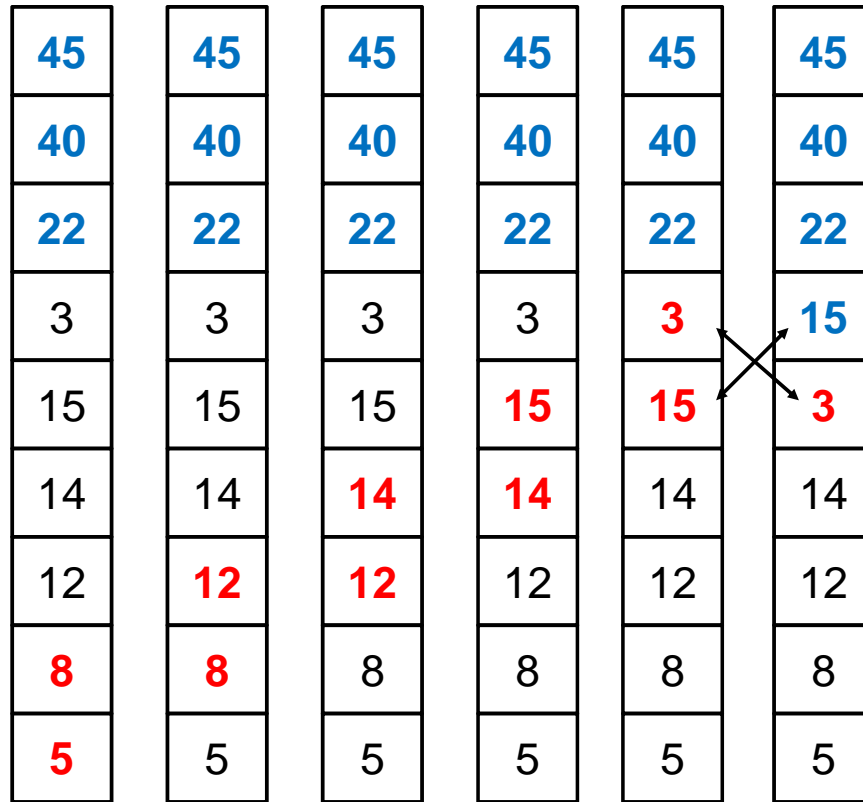
7
c
o
m
p
a
r
i
s
o
n
s

Bubble Sort in Action: Phase 3



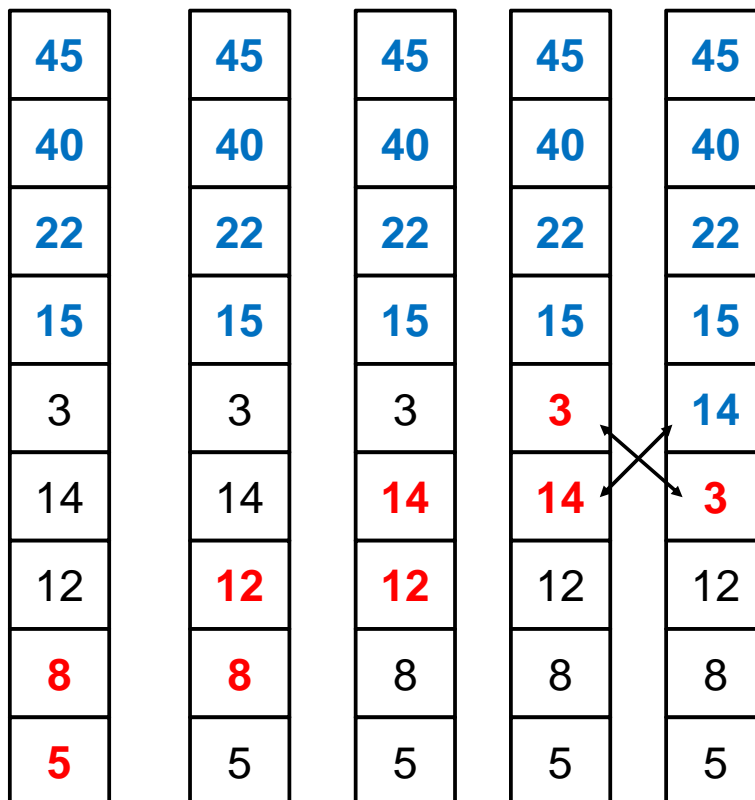
6
c
o
m
p
a
r
i
s
o
n
s

Bubble Sort in Action: Phase 4



5
c
o
m
p
a
r
i
s
o
n
s

Bubble Sort in Action: Phase 5



4
c
o
m
p
a
r
i
s
o
n
s

Bubble Sort in Action: Phase 6

45	45	45	45
40	40	40	40
22	22	22	22
15	15	15	15
14	14	14	14
3	3	3	12
12	12	12	3
8	8	8	8
5	5	5	5

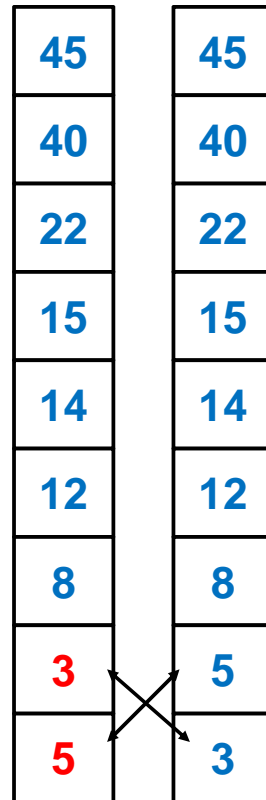
3
c
o
m
p
a
r
i
s
o
n
s

Bubble Sort in Action: Phase 7

45	45	45
40	40	40
22	22	22
15	15	15
14	14	14
12	12	12
3	3	8
8	8	3
5	5	5

2
c
o
m
p
a
r
i
s
o
n
s

Bubble Sort in Action: Phase 8



1
c
o
m
p
a
r
i
s
o
n

Bubble Sort Algorithm in Java

```
void bubbleSort(int List[]){  
    int temp;  
    int size = List.length;  
    for (i = 0; i < size - 1; i++){  
        for (j = 0; j < size - (i + 1); j++){  
            if (List[j] > List[j+1]){  
                temp = List[j];  
                List[j] = List[j+1];  
                List[j+1] = temp;  
            }  
        }  
    }  
}
```

☞ Time complexity of the Bubble Sort algorithm is $O(n^2)$.
Think why?



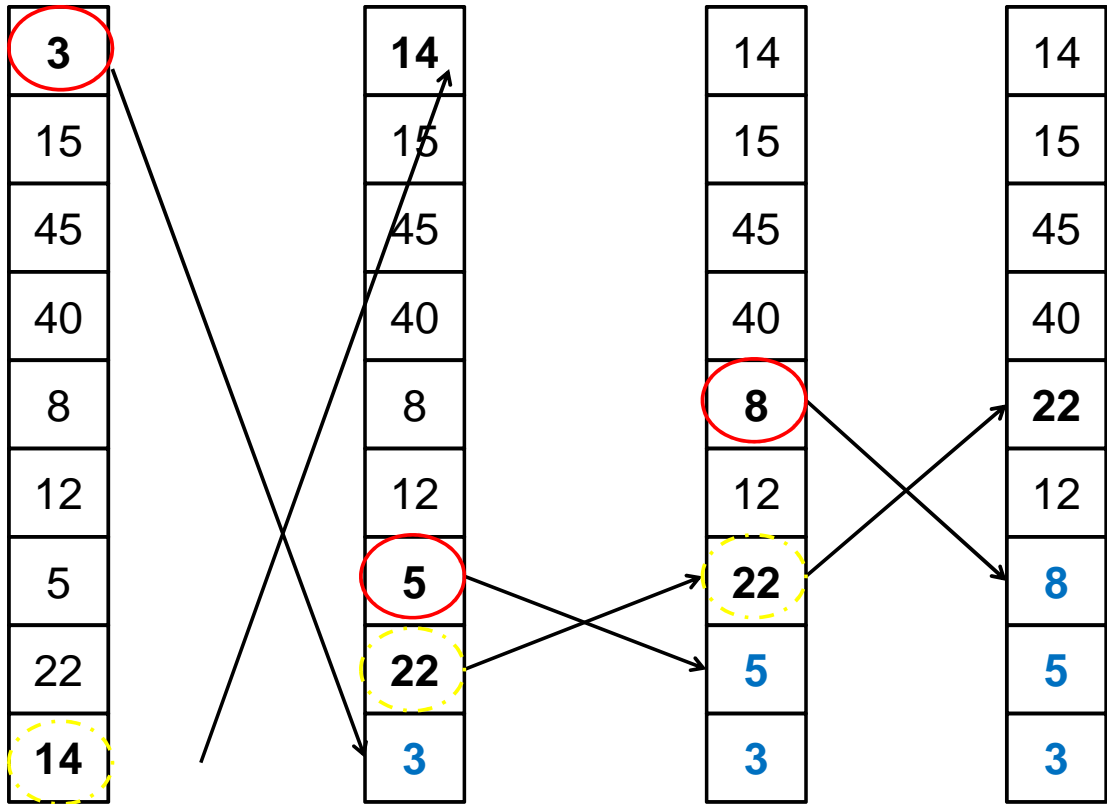
3. Selection Sort



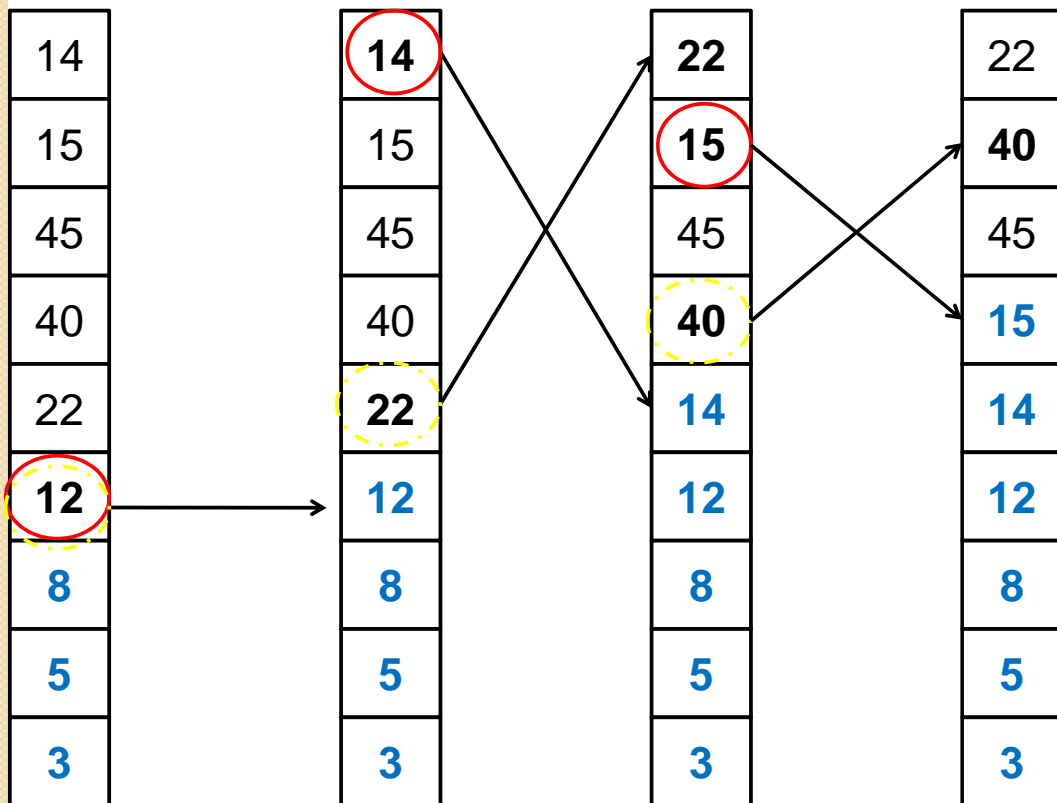
Selection Sort: Algorithm Informal

- Suppose we want to sort an array in ascending order:
 - Locate the smallest element in the array; swap it with element at index 0
 - Then, locate the next smallest element in the array; swap it with element at index 1.
 - Continue until all elements are arranged in order

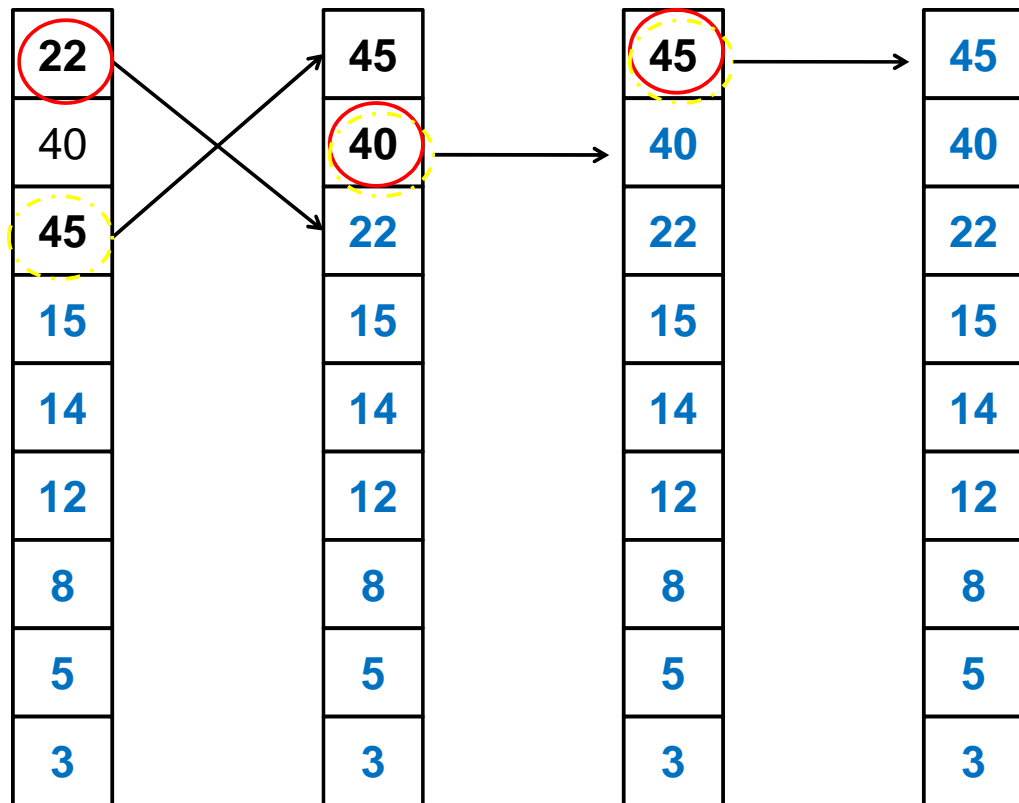
Selection Sort in Action



Selection Sort in Action



Selection Sort in Action



Selection Sort Algorithm in Java

```
void selectionSort(int List[]){  
    int temp, min;  
    int size = List.length;  
    for (i = 0; i < size; i++){  
        min = i;  
        for (j = i + 1; j < size; j++){  
            if (List[j] < List[min]){  
                min = j;  
            }  
        }  
        temp = List[min];  
        List[min] = List[i];  
        List[i] = temp;  
    }  
}
```

☞ Time complexity of the Selection Sort algorithm is $O(n^2)$. Think why?



Bubble Sort vs. Selection Sort

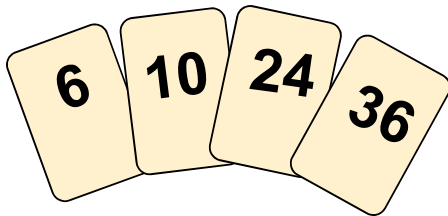
- ❑ Selection Sort is more efficient than Bubble Sort, because of fewer exchanges in the former
- ❑ Both Bubble Sort and Selection Sort belong to the same (quadratic) complexity class ($O(n^2)$)
- ❑ Bubble Sort may be easy to understand as compared to Selection Sort – What do you think?



Insertion Sort

Insertion Sort

Works like someone who **inserts** one more card at a time into a hand of cards that are already **sorted**



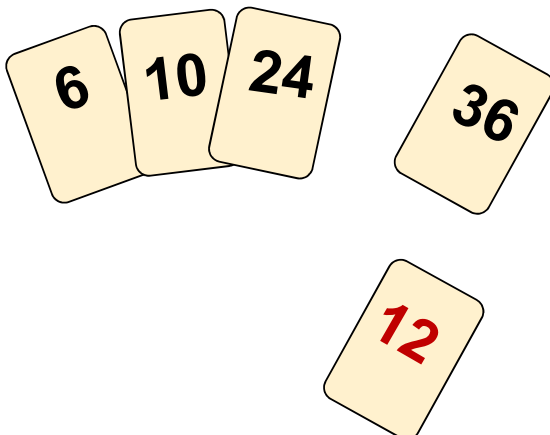
To insert **12**, we need to make room for it ...



24

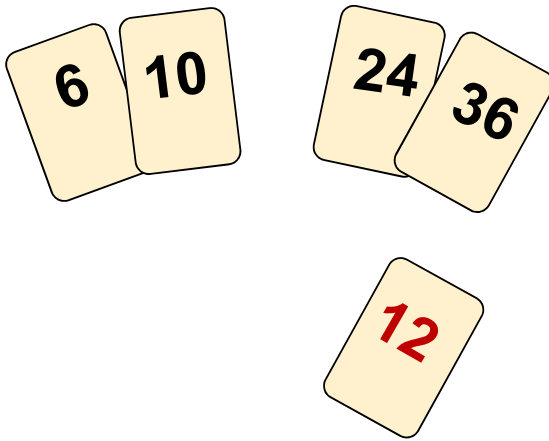
Insertion Sort

... by shifting first 36 towards right...



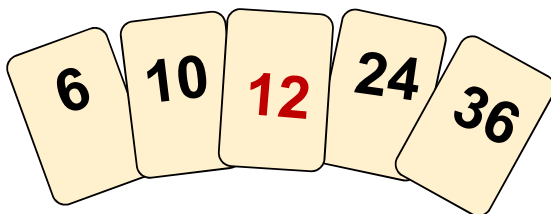
Insertion Sort

... and then shifting 24
towards right



Insertion Sort

Once room is available,
insert the element (12 in this
case)



Insertion Sort: Informal

- We divide the list into two parts: Sorted and Unsorted parts
 - Initially
 - the sorted part contains the first element (at index 0)
 - the unsorted part contains the elements from index 1 to N-1
 - Then, we move element from index 1 to an **appropriate** position in the sorted part, keeping order intact
 - Then, we move element from index 2 to an **appropriate** position in the sorted part, keeping order intact
 - ...
 - Finally, we move element from index N-1 to an **appropriate** position in the sorted part, keeping order intact

Insertion Sort Algorithm in Java

```
void insertionSort(int List[]){
    int temp;
    int size = List.length;
    for (int i = 1; i < size; i++){
        int j = i;
        temp = List[i];
        while (j > 0 && temp < List[j - 1]){
            List[j] = List[j - 1]; // right shifting
            j--;
        }
        List[j] = temp;
    }
}
```

☞ Time complexity of the Insertion Sort algorithm is $O(n^2)$. Think why?