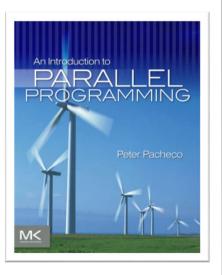


An Introduction to Parallel Programming Peter Pacheco



Chapter 3

Distributed Memory Programming with MPI



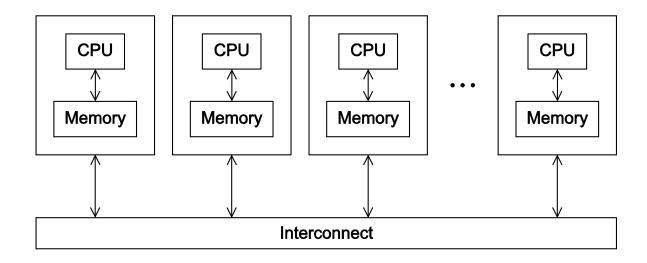
Chapter Subtitle

Roadmap

- Writing your first MPI program.
- Using the common MPI functions.
- The Trapezoidal Rule in MPI.
- Collective communication.
- MPI derived datatypes.
- Performance evaluation of MPI programs.
- Parallel sorting.
- Safety in MPI programs.

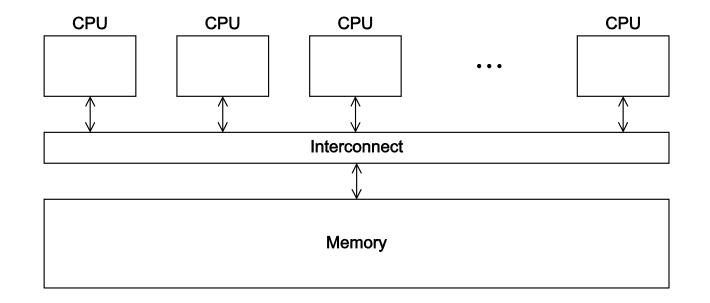


A distributed memory system





A shared memory system





Hello World!

```
#include <stdio.h>
```

```
int main(void) {
    printf("hello, world\n");
```

return 0;



(a classic)



Identifying MPI processes

- Common practice to identify processes by nonnegative integer ranks.
- processes are numbered 0, 1, 2, ... p-1

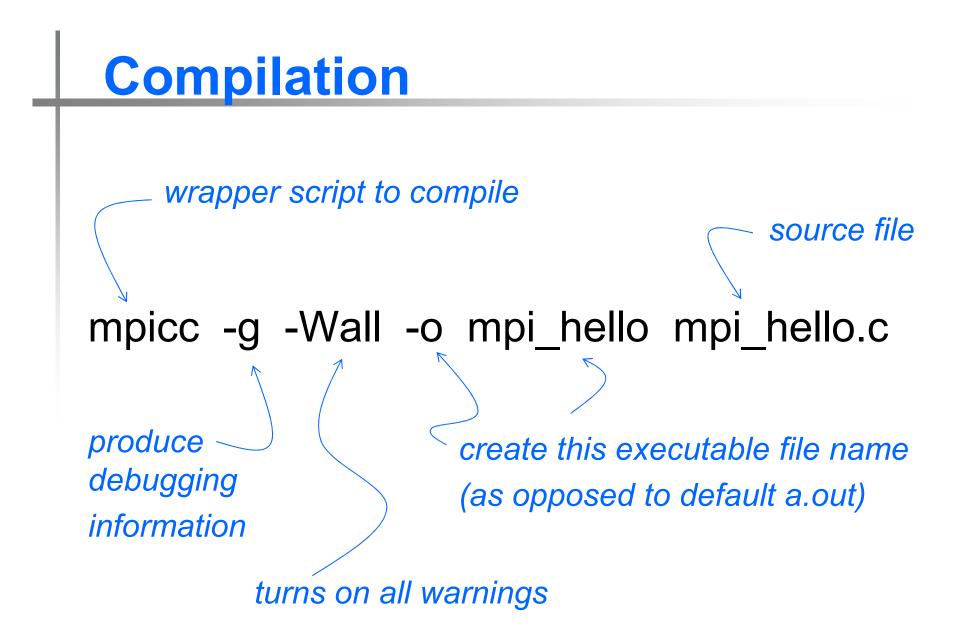


Our first MPI program

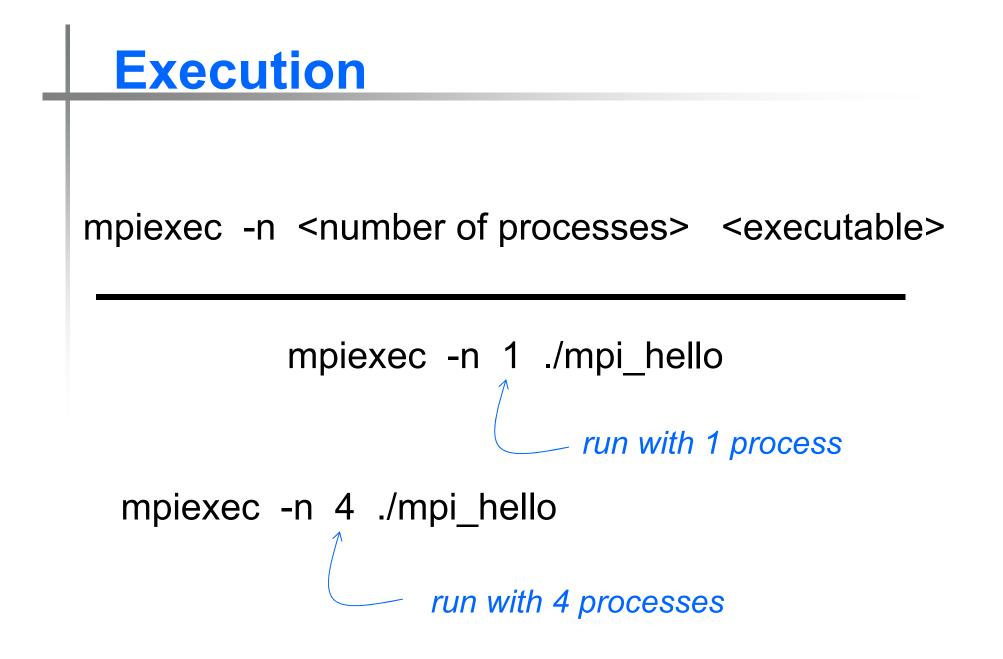
```
1 #include <stdio.h>
2
  #include <string.h> /* For strlen
                     /* For MPI functions, etc */
3 #include <mpi.h>
4
5
   const int MAX_STRING = 100;
6
7
   int main(void) {
8
      char
                 greeting[MAX_STRING];
9
                 comm_sz; /* Number of processes */
      int
10
                 my rank: /* My process rank
      int
                                                    */
11
12
      MPI_Init(NULL, NULL);
13
      MPI Comm size (MPI COMM WORLD, &comm sz);
14
     MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
15
16
      if (my_rank != 0) {
         sprintf(greeting, "Greetings from process %d of %d!",
17
18
               my_rank, comm_sz);
19
         MPI_Send(greeting, strlen(greeting)+1, MPI_CHAR, 0, 0,
20
               MPI COMM WORLD):
21
      } else {
22
         printf("Greetings from process %d of %d!\n", my_rank, comm_sz);
23
         for (int q = 1; q < comm_sz; q++) {
24
            MPI_Recv(greeting, MAX_STRING, MPI_CHAR, q,
25
               0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
26
            printf("%s\n", greeting);
27
28
29
30
      MPI Finalize();
31
      return 0;
32
      /* main */
```













Execution

mpiexec -n 1 ./mpi_hello

Greetings from process 0 of 1 !

mpiexec -n 4 ./mpi_hello

Greetings from process 0 of 4 ! Greetings from process 1 of 4 ! Greetings from process 2 of 4 ! Greetings from process 3 of 4 !



MPI Programs

- Written in C.
 - Has main.
 - Uses stdio.h, string.h, etc.
- Need to add mpi.h header file.
- Identifiers defined by MPI start with "MPI_".
- First letter following underscore is uppercase.
 - For function names and MPI-defined types.
 - Helps to avoid confusion.



MPI Components

MPI_Init

Tells MPI to do all the necessary setup.

int	MPI_Init(
	int*	argc_p	/*	in/out	*/,
	char***	argv_p	/*	in/out	*/);

- MPI_Finalize
 - Tells MPI we're done, so clean up anything allocated for this program.

int MPI_Finalize(void);



Basic Outline

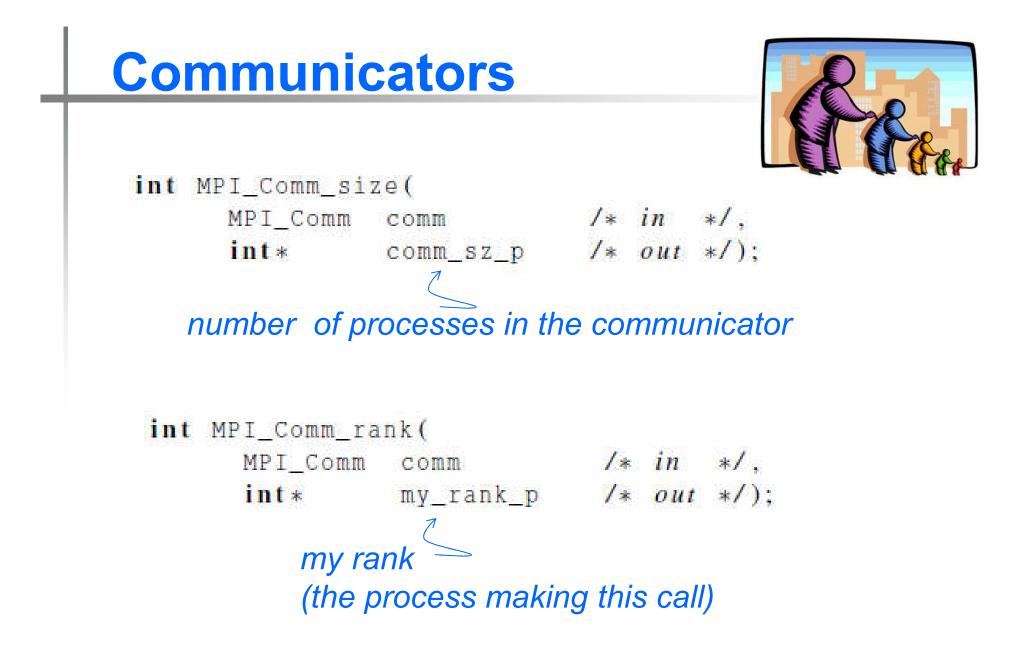
```
SV 8 165
#include <mpi.h>
int main(int argc, char* argv[]) {
   /* No MPI calls before this */
   MPI_Init(&argc, &argv);
   (a) 101 (200)
   MPI_Finalize();
   /* No MPI calls after this */
   8 <u>N</u> 8
   return 0;
}
```



Communicators

- A collection of processes that can send messages to each other.
- MPI_Init defines a communicator that consists of all the processes created when the program is started.
- Called MPI_COMM_WORLD.







SPMD

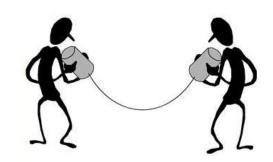
- Single-Program Multiple-Data
- We compile <u>one</u> program.
- Process 0 does something different.
 - Receives messages and prints them while the other processes do the work.
- The if-else construct makes our program SPMD.



Communication

int MPI_Send(

void *	msg_buf_p	/*	in	*/,
int	msg_size	/*	in	*/,
MPI_Datatype	msg_type	/*	in	*/,
int	dest	/*	in	*/,
int	tag	/*	in	*/,
MPI_Comm	communicator	/*	in	*/);





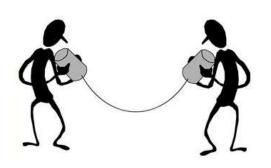
Data types

MPI datatype	C datatype
MPI_CHAR	signed char
MPI_SHORT	signed short int
MPI_INT	signed int
MPI_LONG	signed long int
MPI_LONG_LONG	signed long long int
MPI_UNSIGNED_CHAR	unsigned char
MPI_UNSIGNED_SHORT	unsigned short int
MPI_UNSIGNED	unsigned int
MPI_UNSIGNED_LONG	unsigned long int
MPI_FLOAT	float
MPI_DOUBLE	double
MPI_LONG_DOUBLE	long double
MPI_BYTE	
MPI_PACKED	



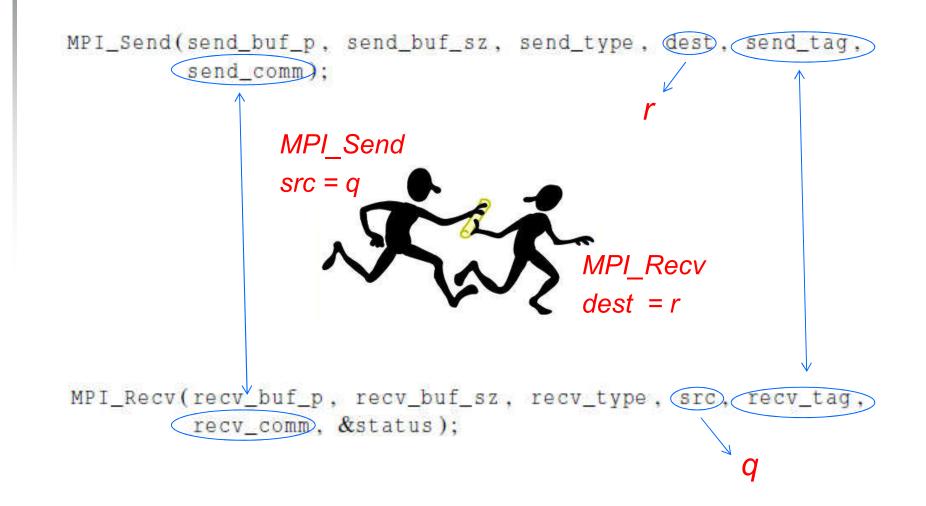
Communication

int MPI_Recv(
void *	msg_buf_p	/*	out	*/,
int	buf_size	/*	in	*/,
MPI_Datatype	<pre>buf_type</pre>	/*	in	*/,
int	source	/*	in	*/,
int	tag	/*	in	*/,
MPI_Comm	communicator	/*	in	*/,
MPI_Status*	status_p	/*	out	*/);





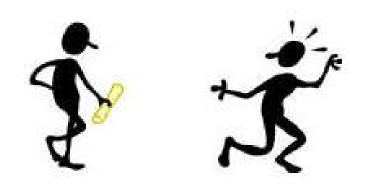
Message matching





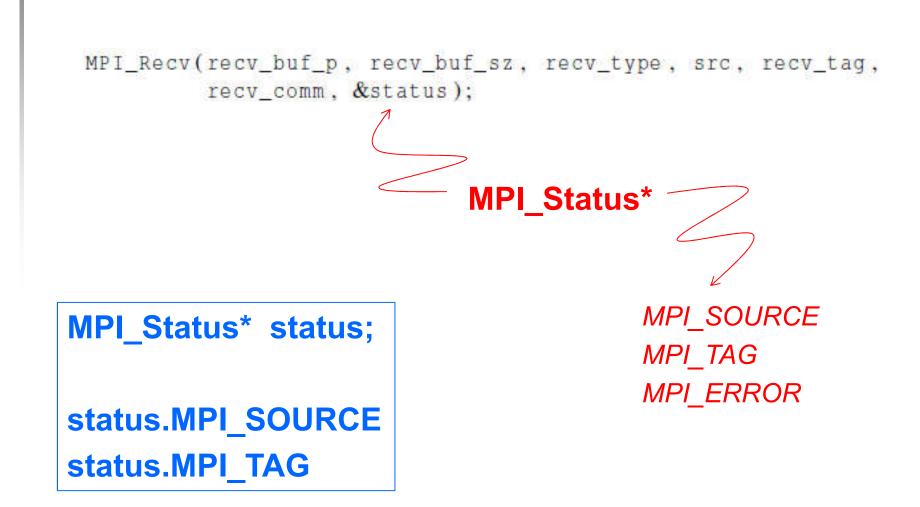
Receiving messages

- A receiver can get a message without knowing:
 - the amount of data in the message,
 - the sender of the message,
 - or the tag of the message.



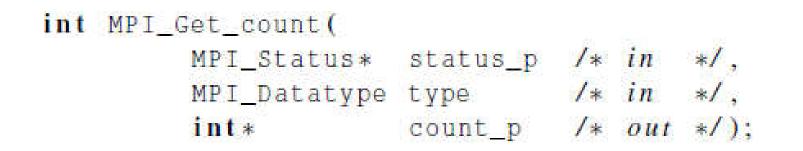


status_p argument





How much data am I receiving?





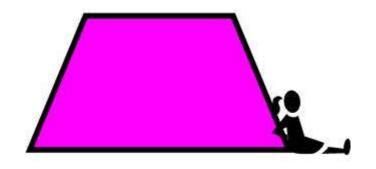


Issues with send and receive

- Exact behavior is determined by the MPI implementation.
- MPI_Send may behave differently with regard to buffer size, cutoffs and blocking.
- MPI_Recv always blocks until a matching message is received.
- Know your implementation; don't make assumptions!





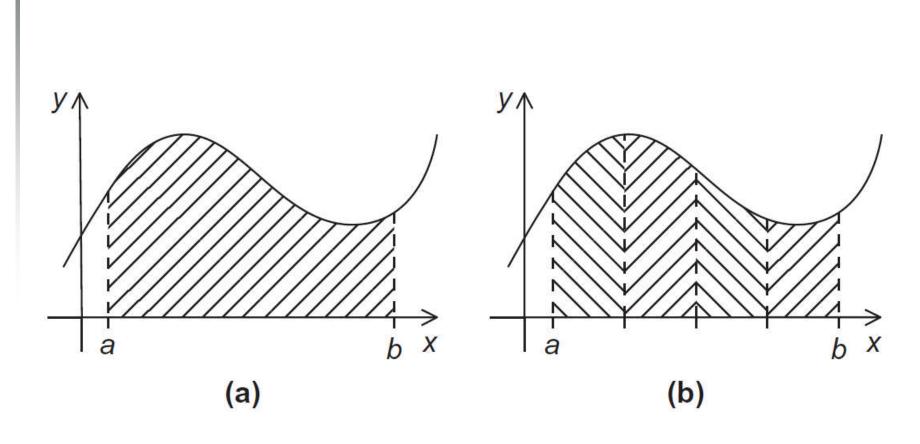


TRAPEZOIDAL RULE IN MPI



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The Trapezoidal Rule





The Trapezoidal Rule

Area of one trapezoid
$$= \frac{h}{2}[f(x_i) + f(x_{i+1})]$$

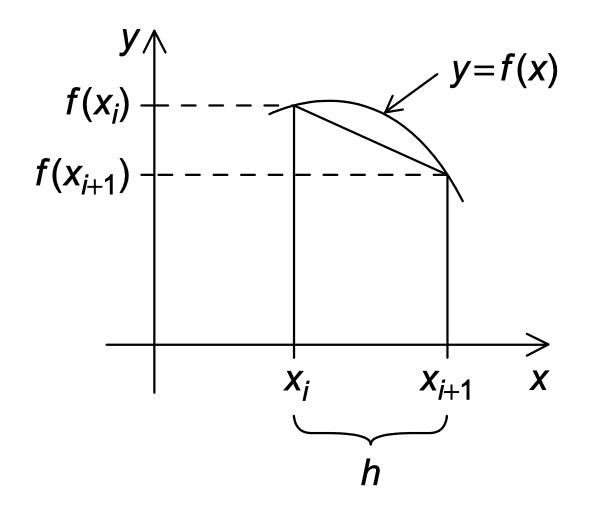
$$h = \frac{b-a}{n}$$

$$x_0 = a, x_1 = a + h, x_2 = a + 2h, \dots, x_{n-1} = a + (n-1)h, x_n = b$$

Sum of trapezoid areas $= h[f(x_0)/2 + f(x_1) + f(x_2) + \dots + f(x_{n-1}) + f(x_n)/2]$



One trapezoid





Pseudo-code for a serial

program

/* Input: a, b, n */
h = (b-a)/n;
approx = (f(a) + f(b))/2.0;
for (i = 0; i <= n-1; i++) {
 x_i = a + i*h;
 approx += f(x_i);
}
approx = h*approx;</pre>



Parallelizing the Trapezoidal Rule

- 1. Partition problem solution into tasks.
- 2. Identify communication channels between tasks.
- 3. Aggregate tasks into composite tasks.
- 4. Map composite tasks to cores.

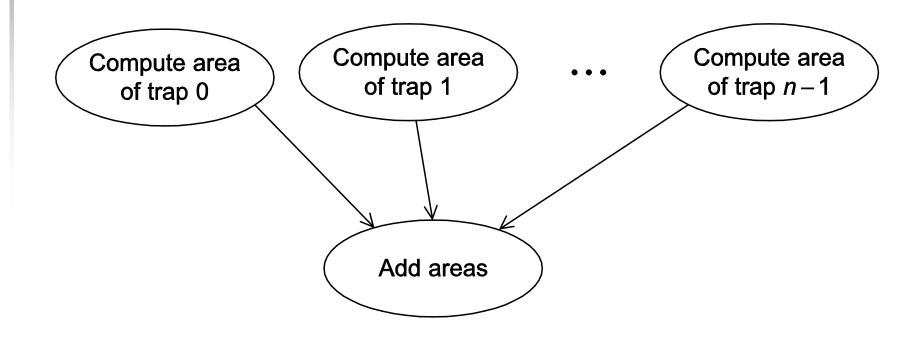


Parallel pseudo-code

```
Get a. b. n:
 2
    h = (b-a)/n;
3
      local n = n/comm sz;
4
      local a = a + my rank*local n*h;
5
      local b = local a + local n*h;
6
      local_integral = Trap(local_a, local_b, local_n, h);
7
      if (my rank != 0)
8
         Send local integral to process 0;
      else /* my_rank == 0 */
9
10
         total_integral = local_integral;
11
         for (proc = 1; proc < comm_sz; proc++) {</pre>
12
            Receive local_integral from proc;
13
            total integral += local integral;
14
15
16
      if (my rank == 0)
         print result;
17
```



Tasks and communications for Trapezoidal Rule





First version (1)

```
int main(void) {
1
2
      int my rank, comm sz, n = 1024, local n;
3
      double a = 0.0, b = 3.0, h, local a, local b;
      double local_int, total_int;
4
5
      int source:
6
7
      MPI Init(NULL, NULL);
8
      MPI Comm rank(MPI COMM WORLD, &my rank);
9
      MPI Comm size (MPI COMM WORLD, &comm sz):
10
      h = (b-a)/n; /* h is the same for all processes */
11
      local n = n/comm sz; /* So is the number of trapezoids */
12
13
14
      local a = a + my rank*local n*h;
      local b = local a + local n*h;
15
16
      local int = Trap(local a, local b, local n, h);
17
      if (my rank != 0) {
18
         MPI_Send(&local_int, 1, MPI_DOUBLE, 0, 0,
19
20
               MPI COMM WORLD):
```



First version (2)

```
21
      } else {
22
         total int = local int;
23
         for (source = 1; source < comm sz; source++) {</pre>
24
            MPI Recv(&local int, 1, MPI DOUBLE, source, 0,
25
                   MPI COMM WORLD, MPI STATUS IGNORE);
26
            total int += local int;
27
28
29
30
      if (my rank == 0) {
31
         printf("With n = %d trapezoids, our estimate\n", n);
32
         printf("of the integral from %f to %f = %.15e\n",
33
              a. b. total int);
34
35
      MPI Finalize();
      return 0;
36
37
     /* main */
```



First version (3)

```
double Trap(
 1
 2
         double left_endpt /* in */,
 3
         double right_endpt /* in */,
4
         int trap_count /* in */,
 5
         double base len /* in */) {
6
      double estimate, x:
 7
      int i:
8
9
      estimate = (f(left_endpt) + f(right_endpt))/2.0;
10
      for (i = 1; i \le trap count - 1; i++)
         x = left endpt + i*base len;
11
12
         estimate += f(x);
13
14
      estimate = estimate*base len;
15
16
      return estimate;
     /* Trap */
17
```



Dealing with I/O

```
#include <stdio.h>
#include <mpi.h>
                                  Each process just
                                  prints a message.
int main(void) {
   int my rank, comm sz;
   MPI Init(NULL, NULL);
   MPI Comm size (MPI COMM WORLD, &comm sz);
   MPI Comm rank (MPI COMM WORLD, &my rank);
   printf("Proc %d of %d > Does anyone have a toothpick?\n",
         my rank, comm sz);
   MPI Finalize();
   return 0;
   /* main */
```



Running with 6 processes

Proc	0	of	6	>	Does	anyone	have	a	toothpick?
Proc	1	of	6	>	Does	anyone	have	a	toothpick?
Proc	2	of	6	>	Does	anyone	have	a	toothpick?
Proc	4	of	6	>	Does	anyone	have	a	toothpick?
Proc	3	of	6	>	Does	anyone	have	а	toothpick?
Proc	5	of	6	>	Does	anyone	have	a	toothpick?

unpredictable output



Input

- Most MPI implementations only allow process 0 in MPI_COMM_WORLD access to stdin.
- Process 0 must read the data (scanf) and send to the other processes.

```
. . .
MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
Get_data(my_rank, comm_sz, &a, &b, &n);
h = (b-a)/n;
. . .
```



Function for reading user input

```
void Get input(
     int my rank /* in */.
         comm_sz /* in */,
     int
     double * a_p /* out */,
     double * b_p /* out */,
     int* n_p
                    /* out */) {
  int dest:
  if (my rank == 0) {
     printf("Enter a, b, and n\n");
     scanf("%lf %lf %d", a p, b p, n p);
     for (dest = 1; dest < comm sz; dest++) {
        MPI_Send(a_p, 1, MPI_DOUBLE, dest, 0, MPI_COMM_WORLD);
        MPI Send(b p, 1, MPI DOUBLE, dest, 0, MPI COMM WORLD);
        MPI Send(n p, 1, MPI INT, dest, 0, MPI COMM WORLD);
  else \{ /* my_rank != 0 */
     MPI_Recv(a p, 1, MPI_DOUBLE, 0, 0, MPI_COMM_WORLD,
           MPI STATUS_IGNORE);
     MPI_Recv(b_p, 1, MPI_DOUBLE, 0, 0, MPI_COMM_WORLD,
           MPI STATUS IGNORE);
     MPI Recv(n p, 1, MPI INT, 0, 0, MPI COMM WORLD,
           MPI STATUS IGNORE);
  /* Get_input */
```



COLLECTIVE COMMUNICATION





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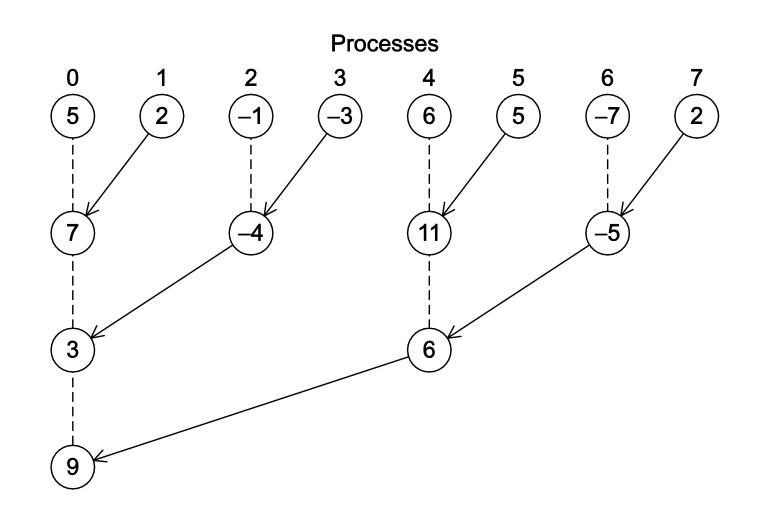
Tree-structured communication

- In the first phase:

 (a) Process 1 sends to 0, 3 sends to 2, 5 sends to 4, and 7 sends to 6.
 (b) Processes 0, 2, 4, and 6 add in the received values.
 (c) Processes 2 and 6 send their new values to processes 0 and 4, respectively.
 (d) Processes 0 and 4 add the received values into their new values.
- 2. (a) Process 4 sends its newest value to process 0.(b) Process 0 adds the received value to its newest value.

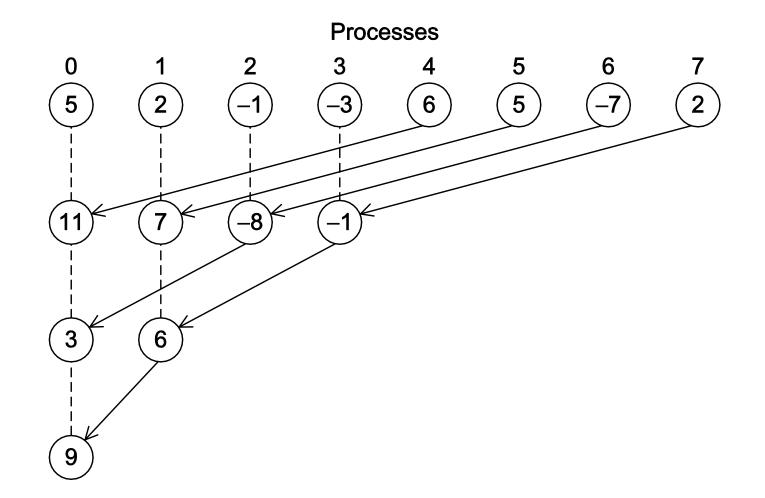


A tree-structured global sum





An alternative tree-structured global sum





MPI_Reduce

void *	input_data_p	/*	in	*/,
void *	output_data_p	/*	out	*/,
int	count	/*	in	*/,
MPI_Datatype	datatype	/*	in	*/,
MPI_Op	operator	/*	in	*/,
int	dest_process	/*	in	*/,
MPI_Comm	comm	/*	in	*/)



Predefined reduction operators

in MPI

Operation Value	Meaning			
MPI_MAX	Maximum			
MPI_MIN	Minimum			
MPI_SUM	Sum			
MPI_PROD Product				
MPI_LAND Logical and				
MPI_BAND	Bitwise and			
MPI_LOR	Logical or			
MPI_BOR	Bitwise or			
MPI_LXOR	Logical exclusive or			
MPI_BXOR	Bitwise exclusive or			
MPI_MAXLOC	Maximum and location of maximum			
MPI_MINLOC	Minimum and location of minimum			



All the processes in the communicator must call the same collective function.

For example, a program that attempts to match a call to MPI_Reduce on one process with a call to MPI_Recv on another process is erroneous, and, in all likelihood, the program will hang or crash.



- The arguments passed by each process to an MPI collective communication must be "compatible."
- For example, if one process passes in 0 as the dest_process and another passes in 1, then the outcome of a call to MPI_Reduce is erroneous, and, once again, the program is likely to hang or crash.



The output_data_p argument is only used on dest_process.

However, all of the processes still need to pass in an actual argument corresponding to output_data_p, even if it's just NULL.



 Point-to-point communications are matched on the basis of tags and communicators.

- Collective communications don't use tags.
- They're matched solely on the basis of the communicator and the order in which they're called.



Example (1)

Time	Process 0	Process 1	Process 2			
0	a = 1; c = 2	a = 1; c = 2	a = 1; c = 2			
1	MPI_Reduce(&a, &b,)	MPI_Reduce(&c, &d,)	MPI_Reduce(&a, &b,)			
2	MPI_Reduce(&c, &d,)	MPI_Reduce(&a, &b,)	MPI_Reduce(&c, &d,)			

Multiple calls to MPI_Reduce





- Suppose that each process calls MPI_Reduce with operator MPI_SUM, and destination process 0.
- At first glance, it might seem that after the two calls to MPI_Reduce, the value of b will be 3, and the value of d will be 6.



Example (3)

 However, the names of the memory locations are irrelevant to the matching of the calls to MPI_Reduce.

The order of the calls will determine the matching so the value stored in b will be 1+2+1 = 4, and the value stored in d will be 2+1+2 = 5.

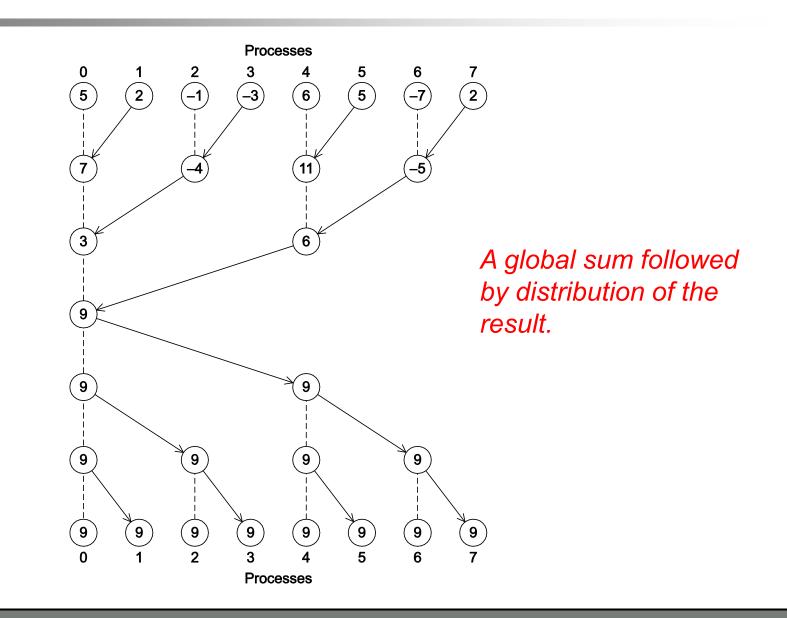


MPI_Allreduce

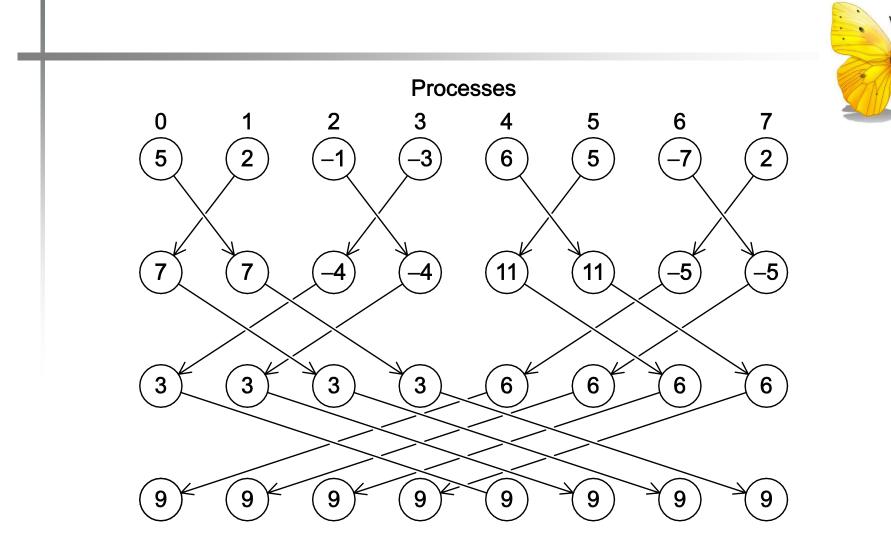
 Useful in a situation in which all of the processes need the result of a global sum in order to complete some larger computation.

```
int MPI_Allreduce(
    void* input_data_p /* in */,
    void* output_data_p /* out */,
    int count /* in */,
    MPI_Datatype datatype /* in */,
    MPI_Op operator /* in */,
    MPI_Comm comm /* in */);
```









A butterfly-structured global sum.

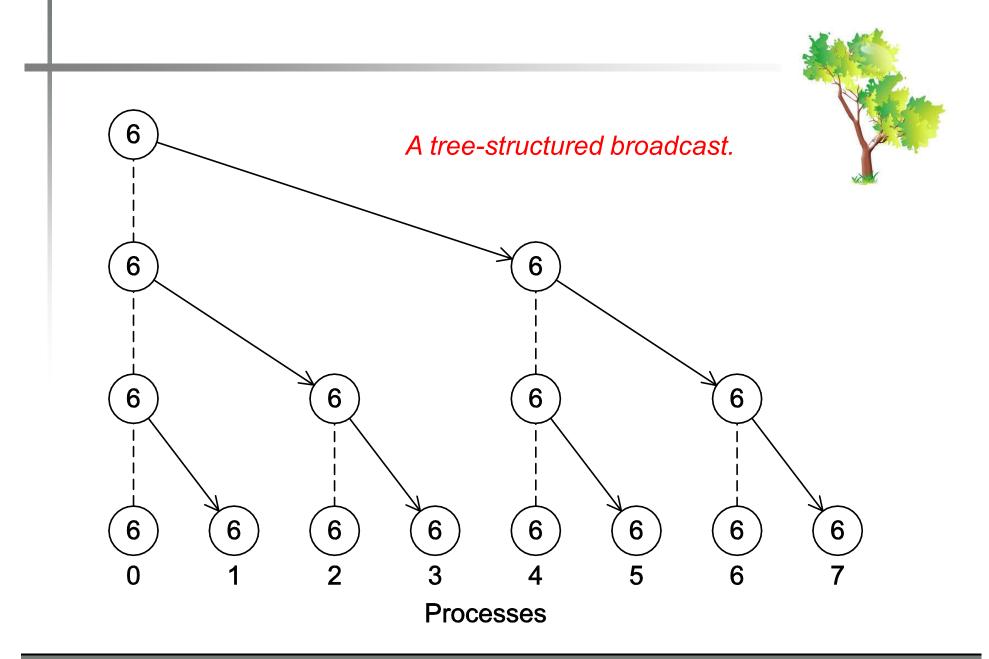


Broadcast

 Data belonging to a single process is sent to all of the processes in the communicator.

<pre>int MPI_Bcast(</pre>				
void *	data_p	/*	in/out	*/,
int	count	/*	in	*/,
MPI_Datatype	datatype	/*	in	*/,
int	source_proc	/*	in	*/,
MPI_Comm	comm	/*	in	*/);







A version of Get_input that uses MPI_Bcast

```
void Get input(
     int my_rank /* in */,
     int comm_sz /* in */,
     double * a_p /* out */,
     double* b_p /* out */,
     int * n_p /* out */) {
  if (my_rank == 0) {
     printf("Enter a, b, and n\n");
     scanf("%lf %lf %d", a_p, b_p, n_p);
  MPI Bcast(a p, 1, MPI DOUBLE, 0, MPI COMM WORLD);
  MPI Bcast(b p, 1, MPI DOUBLE, 0, MPI COMM WORLD);
  MPI Bcast(n_p, 1, MPI INT, 0, MPI COMM WORLD);
 /* Get_input */
```



Data distributions

$$\mathbf{x} + \mathbf{y} = (x_0, x_1, \dots, x_{n-1}) + (y_0, y_1, \dots, y_{n-1})$$

= $(x_0 + y_0, x_1 + y_1, \dots, x_{n-1} + y_{n-1})$
= $(z_0, z_1, \dots, z_{n-1})$
= \mathbf{z}

Compute a vector sum.



Serial implementation of vector addition

void Vector_sum(double x[], double y[], double z[], int n) {
 int i;

for (i = 0; i < n; i++)
 z[i] = x[i] + y[i];
/* Vector_sum */</pre>



Different partitions of a 12component vector among 3 processes

					С	omp	oone	ents				
Process	Block				Cyclic			Block-cyclic $Blocksize = 2$				
0	0	1	2	3	0	3	6	9	0	1	6	7
1	4	5	6	7		4	7	10	2	3	8	9
2	8	9	10	11	2	5	8	11	4	5	10	11



Partitioning options

- Block partitioning
 - Assign blocks of consecutive components to each process.
- Cyclic partitioning
 - Assign components in a round robin fashion.
- Block-cyclic partitioning
 - Use a cyclic distribution of blocks of components.



Parallel implementation of vector addition

```
void Parallel_vector_sum(
    double local_x[] /* in */,
    double local_y[] /* in */,
    double local_z[] /* out */,
    int local_n /* in */) {
    int local_i;

    for (local_i = 0; local_i < local_n; local_i++)
        local_z[local_i] = local_x[local_i] + local_y[local_i];</pre>
```

```
/* Parallel_vector_sum */
```



Scatter

MPI_Scatter can be used in a function that reads in an entire vector on process 0 but only sends the needed components to each of the other processes.

int	MPI_Scatter(

void *	<pre>send_buf_p</pre>	/*	in	*/,
int	send_count	/*	in	*/,
MPI_Datatype	send_type	/*	in	*/,
void *	recv_buf_p	/*	out	*/,
int	recv_count	/*	in	*/,
MPI_Datatype	recv_type	/*	in	*/,
int	src_proc	/*	in	*/,
MPI_Comm	comm	/*	in	*/);



Reading and distributing a vector

```
void Read_vector(
     double local a [] /* out */,
     int local n /* in */,
            n /* in */,
     int
     char vec_name[] /* in */,
     int
          my_rank /* in */,
     MPI Comm comm /* in */) {
  double * a = NULL:
  int i:
  if (my rank == 0) {
     a = malloc(n*sizeof(double));
     printf("Enter the vector %s\n", vec name);
     for (i = 0; i < n; i++)
        scanf("%lf", &a[i]);
     MPI_Scatter(a, local_n, MPI_DOUBLE, local_a, local_n, MPI_DOUBLE,
          0. comm);
     free(a):
  } else {
     MPI Scatter(a, local n, MPI DOUBLE, local a, local n, MPI DOUBLE,
          0. comm):
  /* Read_vector */
```



Gather

 Collect all of the components of the vector onto process 0, and then process 0 can process all of the components.

int	MPI_Gather(
	void *	send_buf_p	/*	in	*/,
	int	send_count	/*	in	*/,
	MPI_Datatype	send_type	/*	in	*/,
	void *	recv_buf_p	/*	out	*/,
	int	recv_count	/*	in	*/,
	MPI_Datatype	recv_type	/*	in	*/,
	int	dest_proc	/*	in	*/,
	MPI_Comm	comm	/*	in	*/);



Print a distributed vector (1)

void	Print_vect	or(
	double	local_b[]	/*	in	*/,
	int	local_n	/*	in	*/,
	int	n	/*	in	*/,
	char	<pre>title[]</pre>	/*	i n	*/,
	int	my_rank	/*	in	*/,
	MPI_Comm	comm	/*	in	*/) {

double* b = NULL; int i;



Print a distributed vector (2)

```
if (my_rank == 0) {
    b = malloc(n*sizeof(double));
    MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE,
        0, comm);
    printf("%s\n", title);
    for (i = 0; i < n; i++)
        printf("%f ", b[i]);
    printf("\n");
    free(b);
} else {
    MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE,
        0, comm);
}
/* Print_vector */</pre>
```

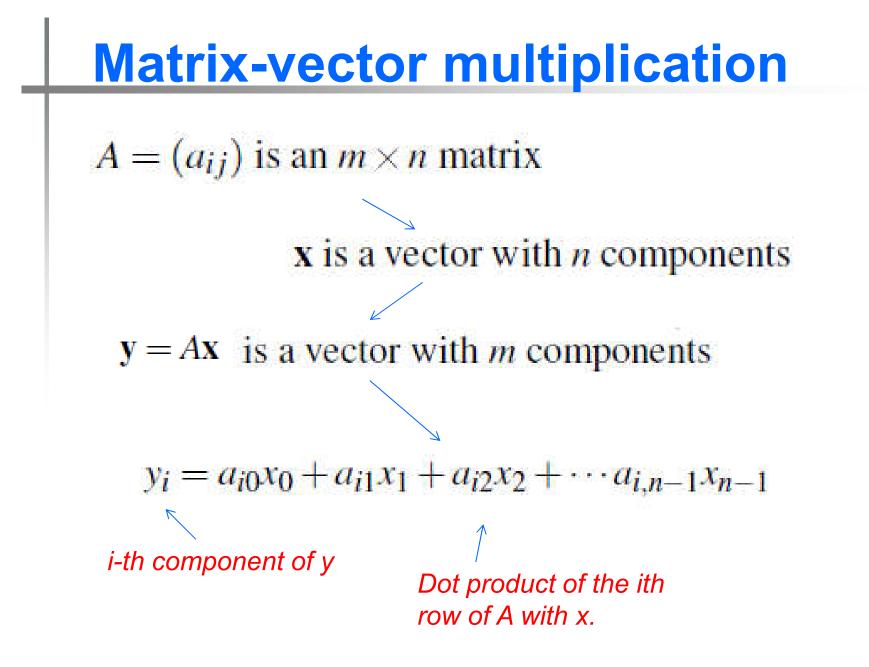


Allgather

- Concatenates the contents of each process' send_buf_p and stores this in each process' recv_buf_p.
- As usual, recv_count is the amount of data being received from each process.

int	MPI_Allgather(
	void *	<pre>send_buf_p</pre>	/*	in	*/,
	int	send_count	/*	in	*/,
	MPI_Datatype	send_type	/*	in	*/,
	void *	recv_buf_p	/*	out	*/,
	int	recv_count	/*	in	*/,
	MPI_Datatype	recv_type	/*	in	*/,
	MPI_Comm	comm	/*	in	*/);







Matrix-vector multiplication

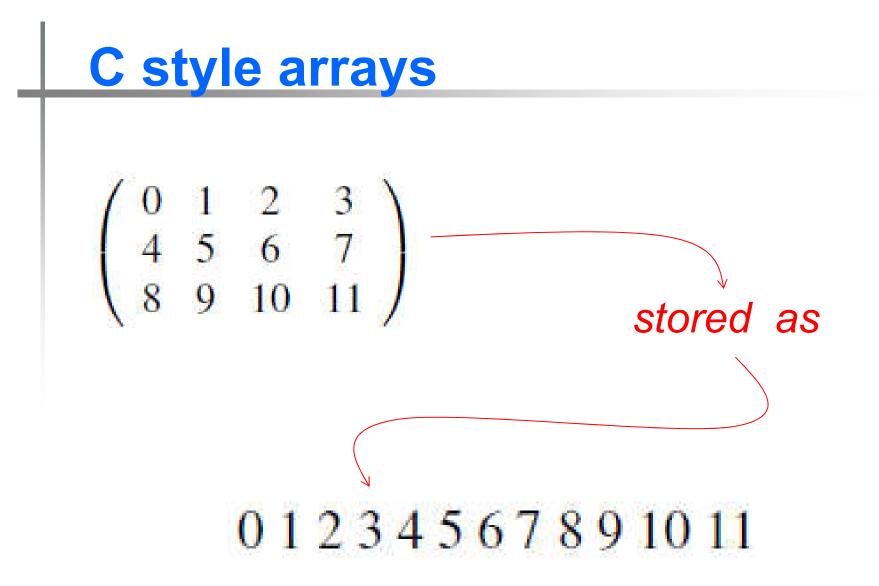
<i>a</i> 00	<i>a</i> 01	• • •	<i>a</i> _{0,<i>n</i>-1}		yo
<i>a</i> ₁₀	<i>a</i> ₁₁	• • •	$a_{1,n-1}$	xo	Y1
:	3		:	<i>x</i> ₁	÷
a_{i0}	a_{i1}	•••	$a_{i,n-1}$: =	$y_i = a_{i0}x_0 + a_{i1}x_1 + \cdots + a_{i,n-1}x_{n-1}$
:	3		:	x_{n-1}	1
$a_{m-1,0}$	$a_{m-1,1}$		$a_{m-1,n-1}$		<i>Ут</i> -1



Multiply a matrix by a vector

Serial pseudo-code







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Serial matrix-vector multiplication

```
void Mat_vect_mult(
     double A[] /* in */,
     double x[] /* in */,
     double y[] /* out */,
     int m /* in */,
     int n /* in */) {
  int i, j;
  for (i = 0; i < m; i++) {
     y[i] = 0.0;
     for (j = 0; j < n; j++)
        y[i] += A[i*n+j]*x[j];
  /* Mat_vect_mult */
```



An MPI matrix-vector multiplication function (1)

void Mat_vect_mu	ult(
double	local_A[]	/*	in	*/,
double	local_x[]	/*	in	*/,
double	local_y[]	/*	out	*/,
int	local_m	/*	in	*/,
int	n	/*	in	*/,
int	local_n	/*	in	*/,
MPI_Comm	comm	/*	in	*/)
double * x;				
<pre>int local_i,</pre>	j;			
int local_ok	= 1;			



```
An MPI matrix-vector
multiplication function (2)
 x = malloc(n*sizeof(double));
 MPI_Allgather(local_x, local_n, MPI_DOUBLE,
       x, local n, MPI DOUBLE, comm);
 for (local_i = 0; local_i < local_m; local_i++) {</pre>
    local_y[local_i] = 0.0;
    for (j = 0; j < n; j++)
       local_y[local_i] += local_A[local_i*n+j]*x[j];
 free(x);
 /* Mat_vect_mult */
```





MPI DERIVED DATATYPES



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Derived datatypes

- Used to represent any collection of data items in memory by storing both the types of the items and their relative locations in memory.
- The idea is that if a function that sends data knows this information about a collection of data items, it can collect the items from memory before they are sent.
- Similarly, a function that receives data can distribute the items into their correct destinations in memory when they're received.



Derived datatypes

 Formally, consists of a sequence of basic MPI data types together with a displacement for each of the data types.

Trapezoidal Rule example:

Variable	Address
a	24
b	40
n	48

 $\{(MPI_DOUBLE, 0), (MPI_DOUBLE, 16), (MPI_INT, 24)\}$



MPI_Type create_struct

 Builds a derived datatype that consists of individual elements that have different basic types.

<pre>int MPI_Type_create_</pre>	struct(
int	count	/*	in	*/,
int	<pre>array_of_blocklengths[]</pre>	/*	in	*/,
MPI_Aint	<pre>array_of_displacements[]</pre>	/*	in	*/,
MPI_Datatype	<pre>array_of_types[]</pre>	/*	in	*/,
MPI_Datatype*	new_type_p	/*	out	*/);



MPI_Get_address

- Returns the address of the memory location referenced by location_p.
- The special type MPI_Aint is an integer type that is big enough to store an address on the system.

int MPI_Get_address(void * location_p /* in */, MPI_Aint* address_p /* out */);



MPI_Type_commit

 Allows the MPI implementation to optimize its internal representation of the datatype for use in communication functions.

int MPI_Type_commit(MPI_Datatype* new_mpi_t_p /* in/out */);



MPI_Type_free

When we're finished with our new type, this frees any additional storage used.

int MPI_Type_free(MPI_Datatype* old_mpi_t_p /* in/out */);



Get input function with a derived datatype (1)

void	<pre>Build_mpi_type(</pre>					
	double *	a_p	/*	in	*/,	
	double *	b_p	/*	in	*/,	
	int*	n_p	/*	in	*/,	
	MPI_Datatype*	input_mpi_t_p	/*	out	*/)	{

int array_of_blocklengths[3] = {1, 1, 1}; MPI_Datatype array_of_types[3] = {MPI_DOUBLE, MPI_DOUBLE, MPI_INT}; MPI_Aint a_addr, b_addr, n_addr; MPI_Aint array_of_displacements[3] = {0};



Get input function with a derived datatype (2)

```
MPI_Get_address(a_p, &a_addr);
MPI_Get_address(b_p, &b_addr);
MPI_Get_address(n_p, &n_addr);
array_of_displacements[1] = b_addr-a_addr;
array_of_displacements[2] = n_addr-a_addr;
MPI_Type_create_struct(3, array_of_blocklengths,
array_of_displacements, array_of_types,
input_mpi_t_p);
MPI_Type_commit(input_mpi_t_p);
/* Build_mpi_type */
```



Get input function with a derived datatype (3)

Build_mpi_type(a_p, b_p, n_p, &input_mpi_t);

```
if (my_rank == 0) {
    printf("Enter a, b, and n\n");
    scanf("%lf %lf %d", a_p, b_p, n_p);
}
MPI_Bcast(a_p, 1, input_mpi_t, 0, MPI_COMM_WORLD);
MPI_Type_free(&input_mpi_t);
/* Get_input */
```





PERFORMANCE EVALUATION



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Elapsed parallel time

Returns the number of seconds that have elapsed since some time in the past.

```
double MPI_Wtime(void);
    double start, finish;
    . . .
    start = MPI_Wtime();
    /* Code to be timed */
    . . .
    finish = MPI_Wtime();
    printf("Proc %d > Elapsed time = %e seconds\n"
        my_rank, finish-start);
```



Elapsed serial time

- In this case, you don't need to link in the MPI libraries.
- Returns time in microseconds elapsed from some point in the past.

```
#include "timer.h"
. . .
double now;
. . .
GET_TIME(now);
```





Elapsed serial time

```
#include "timer.h"
. . .
double start, finish;
. . .
GET_TIME(start);
/* Code to be timed */
. . .
GET_TIME(finish);
printf("Elapsed time = %e seconds\n", finish-start);
```



MPI_Barrier

Ensures that no process will return from calling it until every process in the communicator has started calling it.

int MPI_Barrier(MPI_Comm comm /* in */);





MPI_Barrier

```
double local_start, local_finish, local_elapsed, elapsed;
. . . .
MPI_Barrier(comm);
local_start = MPI_Wtime();
/* Code to be timed */
. . .
local finish = MPI Wtime();
local_elapsed = local_finish - local_start;
MPI_Reduce(&local_elapsed, &elapsed, 1, MPI_DOUBLE,
   MPI MAX, 0, comm):
if (my rank == 0)
   printf("Elapsed time = %e seconds\n", elapsed);
```



Run-times of serial and parallel matrix-vector multiplication

	Order of Matrix				
comm_sz	1024	2048	4096	8192	16,384
1	4.1	16.0	64.0	270	1100
2	2.3	8.5	33.0	140	560
4	2.0	5.1	18.0	70	280
8	1.7	3.3	9.8	36	140
16	1.7	2.6	5.9	19	71

(Seconds)



Speedup

$$S(n,p) = \frac{T_{\text{serial}}(n)}{T_{\text{parallel}}(n,p)}$$



Efficiency

$$E(n,p) = \frac{S(n,p)}{p} = \frac{T_{\text{serial}}(n)}{p \times T_{\text{parallel}}(n,p)}$$



Speedups of Parallel Matrix-Vector Multiplication

	Order of Matrix					
comm_sz	1024	2048	4096	8192	16,384	
1	1.0	1.0	1.0	1.0	1.0	
2	1.8	1.9	1.9	1.9	2.0	
4	2.1	3.1	3.6	3.9	3.9	
8	2.4	4.8	6.5	7.5	7.9	
16	2.4	6.2	10.8	14.2	15.5	



Efficiencies of Parallel Matrix-Vector Multiplication

8	Order of Matrix					
comm_sz	1024	2048	4096	8192	16,384	
1	1.00	1.00	1.00	1.00	1.00	
2	0.89	0.94	0.97	0.96	0.98	
4	0.51	0.78	0.89	0.96	0.98	
8	0.30	0.61	0.82	0.94	0.98	
16	0.15	0.39	0.68	0.89	0.97	



Scalability

A program is scalable if the problem size can be increased at a rate so that the efficiency doesn't decrease as the number of processes increase.





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Scalability

- Programs that can maintain a constant efficiency without increasing the problem size are sometimes said to be strongly scalable.
- Programs that can maintain a constant efficiency if the problem size increases at the same rate as the number of processes are sometimes said to be weakly scalable.



A PARALLEL SORTING ALGORITHM



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Sorting

- n keys and p = comm sz processes.
- n/p keys assigned to each process.
- No restrictions on which keys are assigned to which processes.
- When the algorithm terminates:
 - The keys assigned to each process should be sorted in (say) increasing order.
 - If 0 ≤ q < r < p, then each key assigned to process q should be less than or equal to every key assigned to process r.



Serial bubble sort

```
void Bubble_sort(
     int a[] /* in/out */,
     int n /* in */) {
  int list_length, i, temp;
  for (list_length = n; list_length >= 2; list_length--)
     for (i = 0; i < list_length - 1; i++)
        if (a[i] > a[i+1]) {
           temp = a[i];
           a[i] = a[i+1];
           a[i+1] = temp;
  /* Bubble_sort */
```



Odd-even transposition sort

- A sequence of phases.
- Even phases, compare swaps:

 $(a[0], a[1]), (a[2], a[3]), (a[4], a[5]), \dots$

Odd phases, compare swaps:

 $(a[1], a[2]), (a[3], a[4]), (a[5], a[6]), \ldots$



Example

Start: 5, 9, 4, 3 Even phase: compare-swap (5,9) and (4,3) getting the list 5, 9, 3, 4 Odd phase: compare-swap (9,3) getting the list 5, 3, 9, 4 Even phase: compare-swap (5,3) and (9,4) getting the list 3, 5, 4, 9 Odd phase: compare-swap (5,4) getting the list 3, 4, 5, 9



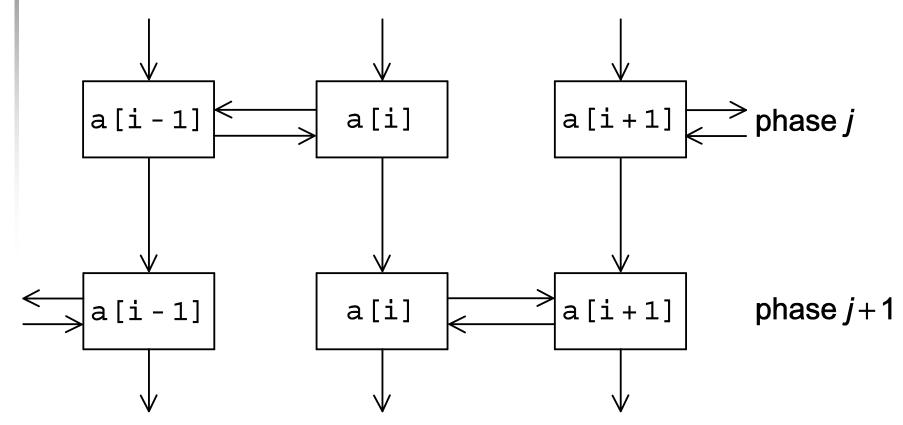
Serial odd-even transposition

sort

```
void Odd_even_sort(
      int a [] /* in/out */,
      int n /* in */) {
   int phase, i, temp;
   for (phase = 0; phase < n; phase++)
      if (phase % 2 == 0) { /* Even phase */
         for (i = 1; i < n; i += 2)
            if (a[i-1] > a[i]) {
              temp = a[i];
               a[i] = a[i-1];
              a[i-1] = temp;
      } else { /* Odd phase */
         for (i = 1; i < n-1; i += 2)
            if (a[i] > a[i+1]) {
               temp = a[i];
               a[i] = a[i+1];
               a[i+1] = temp;
   /* Odd_even_sort */
```



Communications among tasks in odd-even sort



Tasks determining a[i] are labeled with a[i].



Parallel odd-even transposition

sort

Time	Process						
	0	1	2	3			
Start	15, 11, 9, 16	3, 14, 8, 7	4, 6, 12, 10	5, 2, 13, 1			
After Local Sort	9, 11, 15, 16	3, 7, 8, 14	4, 6, 10, 12	1, 2, 5, 13			
After Phase 0	3, 7, 8, 9	11, 14, 15, 16	1, 2, 4, 5	6, 10, 12, 13			
After Phase 1	3, 7, 8, 9	1, 2, 4, 5	11, 14, 15, 16	6, 10, 12, 13			
After Phase 2	1, 2, 3, 4	5, 7, 8, 9	6, 10, 11, 12	13, 14, 15, 16			
After Phase 3	1, 2, 3, 4	5, 6, 7, 8	9, 10, 11, 12	13, 14, 15, 16			



Pseudo-code

```
Sort local keys;
for (phase = 0; phase < comm_sz; phase++) {
    partner = Compute_partner(phase, my_rank);
    if (I'm not idle) {
        Send my keys to partner;
        Receive keys from partner;
        if (my_rank < partner)
            Keep smaller keys;
        else
            Keep larger keys;
    }
}</pre>
```



Compute_partner

if (phase % 2 == 0) /* Even phase */ if (my_rank % 2 != 0) /* Odd rank */ partner = $my_rank - 1;$ /* Even rank */ else partner = $my_rank + 1$; else /* Odd phase */ if (my rank % 2 != 0) /* Odd rank */ $partner = my_rank + 1;$ /* Even rank */ else partner = $my_rank - 1$; if (partner == -1 || partner == comm_sz) partner = MPI_PROC_NULL;



- The MPI standard allows MPI_Send to behave in two different ways:
 - it can simply copy the message into an MPI managed buffer and return,
 - or it can block until the matching call to MPI_Recv starts.



- Many implementations of MPI set a threshold at which the system switches from buffering to blocking.
- Relatively small messages will be buffered by MPI_Send.
- Larger messages, will cause it to block.



- If the MPI_Send executed by each process blocks, no process will be able to start executing a call to MPI_Recv, and the program will hang or deadlock.
- Each process is blocked waiting for an event that will never happen.

(see pseudo-code)



- A program that relies on MPI provided buffering is said to be unsafe.
- Such a program may run without problems for various sets of input, but it may hang or crash with other sets.



MPI_Ssend

- An alternative to MPI_Send defined by the MPI standard.
- The extra "s" stands for synchronous and MPI_Ssend is guaranteed to block until the matching receive starts.

<pre>int MPI_Ssend(</pre>				
void *	msg_buf_p	/*	in	*/,
int	msg_size	/*	in	*/,
MPI_Datatype	msg_type	/*	in	*/,
int	dest	/*	in	*/,
int	tag	/*	in	*/,
MPI_Comm	communicator	/*	in	*/);



Restructuring communication

MPI_Send(msg, size, MPI_INT, (my_rank+1) % comm_sz, 0, comm); MPI_Recv(new_msg, size, MPI_INT, (my_rank+comm_sz-1) % comm_sz, 0, comm, MPI_STATUS_IGNORE.



```
if (my_rank % 2 == 0) {
    MPI_Send(msg, size, MPI_INT, (my_rank+1) % comm_sz, 0, comm);
    MPI_Recv(new_msg, size, MPI_INT, (my_rank+comm_sz-1) % comm_sz,
            0, comm, MPI_STATUS_IGNORE.
} else {
    MPI_Recv(new_msg, size, MPI_INT, (my_rank+comm_sz-1) % comm_sz,
            0, comm, MPI_STATUS_IGNORE.
    MPI_Send(msg, size, MPI_INT, (my_rank+1) % comm_sz, 0, comm);
}
```



MPI_Sendrecv

- An alternative to scheduling the communications ourselves.
- Carries out a blocking send and a receive in a single call.
- The dest and the source can be the same or different.
- Especially useful because MPI schedules the communications so that the program won't hang or crash.



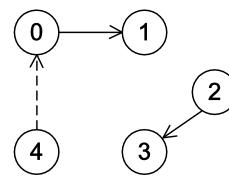
MPI_Sendrecv

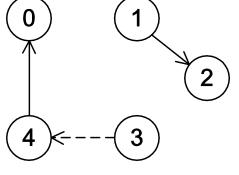
<pre>send_buf_p</pre>	/*	in	*/,
<pre>send_buf_size</pre>	/*	in	*/,
<pre>send_buf_type</pre>	/*	in	*/,
dest	/*	in	*/,
send_tag	/*	in	*/,
recv_buf_p	/*	out	*/,
recv_buf_size	/*	i n	*/,
recv_buf_type	/*	in	*/,
source	/*	in	*/,
recv_tag	/*	in	*/,
communicator	/*	in	*/,
status_p	/*	in	*/);
	<pre>send_buf_size send_buf_type dest send_tag recv_buf_p recv_buf_size recv_buf_type source recv_tag communicator</pre>	<pre>send_buf_size /* send_buf_type /* dest /* send_tag /* recv_buf_p /* recv_buf_size /* recv_buf_type /* source /* recv_tag /* communicator /*</pre>	<pre>send_buf_size /* in send_buf_type /* in dest /* in send_tag /* in recv_buf_p /* out recv_buf_size /* in recv_buf_type /* in source /* in recv_tag /* in communicator /* in</pre>



Safe communication with five

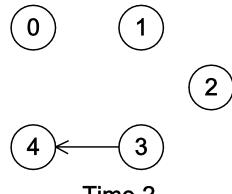
processes





Time 0





Time 2



Parallel odd-even transposition sort

```
void Merge low(
     int my_keys[], /* in/out */
     int recv_keys[], /* in */
     int temp_keys[], /* scratch */
     int local_n /* = n/p, in */ {
  int mi, ri, ti;
  mi = ri = ti = 0;
  while (t_i < local_n) {</pre>
     if (my keys[m i] <= recv keys[r i]) {</pre>
       temp keys[t i] = my keys[m i];
        t i++; m i++;
     } else {
       temp keys[t_i] = recv_keys[r_i];
       t i++; r i++;
  for (m i = 0; m i < local n; m i++)
     my keys[m i] = temp keys[m i];
 /* Merge_low */
```



Run-times of parallel odd-even

sort

Processes	Number of Keys (in thousands)				
	200	400	800	1600	3200
1	88	190	390	830	1800
2	43	91	190	410	860
4	22	46	96	200	430
8	12	24	51	110	220
16	7.5	14	29	60	130

(times are in milliseconds)



Concluding Remarks (1)

- MPI or the Message-Passing Interface is a library of functions that can be called from C, C++, or Fortran programs.
- A communicator is a collection of processes that can send messages to each other.
- Many parallel programs use the singleprogram multiple data or SPMD approach.



Concluding Remarks (2)

- Most serial programs are deterministic: if we run the same program with the same input we'll get the same output.
- Parallel programs often don't possess this property.
- Collective communications involve all the processes in a communicator.



Concluding Remarks (3)

- When we time parallel programs, we're usually interested in elapsed time or "wall clock time".
- Speedup is the ratio of the serial run-time to the parallel run-time.
- Efficiency is the speedup divided by the number of parallel processes.



Concluding Remarks (4)

- If it's possible to increase the problem size (n) so that the efficiency doesn't decrease as p is increased, a parallel program is said to be scalable.
- An MPI program is unsafe if its correct behavior depends on the fact that MPI_Send is buffering its input.

