

Classic Cryptosystems

Key Points

- Field: set of elements with $+$ & $*$
- Modular Arithmetic: reduces all numbers to fixed set $[0...n-1]$
- GCD: largest positive integer dividing
- Finite Field: finite number of elements
- Order Finite Field: power of a prime p^n
where $n = \text{integer}$
- Finite Field: of order p can be defined using normal arithmetic mod p

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Modulo Operation

- ✦ Q: What is $12 \bmod 9$?
- ✦ A: $12 \bmod 9 \equiv 3$
- ✦ Let $a, r, m \in \mathbb{Z}$
 (\mathbb{Z} = set of all integers) and $m > 0$.
 We write
- ✦ $r \equiv a \bmod m$ if $m-r$ divides a .
- ✦ m is called the modulus.
- ✦ r is called the remainder.

$$q \cdot a = m - r \qquad 0 \leq r < m$$

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Ring

- ✦ Ring Z_m is:
 - Set of integers: $Z_m = \{0, 1, 2, \dots, m-1\}$
 - Two operation: "+" and "×"
 - ✦ "+" $\rightarrow a + b \equiv c \bmod m$ ($c \in Z_m$)
 - ✦ "×" $\rightarrow a \times b \equiv d \bmod m$ ($d \in Z_m$)
- ✦ **Example:**
 - $m = 7$, $Z_7 = \{0, 1, 2, 3, 4, 5, 6\}$
 - ✦ $6 + 5 = 11 \bmod 7 = 4$
 - ✦ $6 \times 5 = 30 \bmod 7 = 2$

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Ring Z_m Properties & Operations

- ✦ Identity: additive '0', multiplicative '1'
 $a+0=a$, $a \times 1 = a \bmod m$
- ✦ Inverse: additive '-a', multiplicative ' a^{-1} '
 $a+(-a)=0 \bmod m$, $a \times a^{-1} = 1 \bmod m$
Multiplicative inverse exist if $\gcd(a, m) = 1$
- ✦ *Ring Addition and Multiplication is:
 Closed, Commutative, Associative*

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Division on Ring Z_m

Ring Division: $4/15 \bmod 26$???

- ✦ $4/15 \bmod 26 = 4 \times 15^{-1} \bmod 26$
- ✦ $15^{-1} \bmod 26$ exist if $\gcd(15, 26)=1$
- ✦ $15^{-1} \bmod 26 = 7$
- ➔ $4/15 \bmod 26 = 4 \times 7 \bmod 26 = 28 \bmod 26 = 2$

Note that the modulo operation can be applied whenever we want:

- ✦ $(a + b) \bmod m = [(a \bmod m) + (b \bmod m)] \bmod m$
- ✦ $(a \times b) \bmod m = [(a \bmod m) \times (b \bmod m)] \bmod m$

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Exponentiation in Z_m

Ring Exponentiation: $3^8 \bmod 7 = ???$

- ✦ $3^8 \bmod 7 = 6561 \bmod 7$
- ✦ $6561 \bmod 7 = 2 \rightarrow 6561 = (937 \times 7) + 2$
- ✦ Or $= 3^8 = 3^4 \times 3^4 = 3^2 \times 3^2 \times 3^2 \times 3^2$
- ✦ $3^8 \bmod 7 = [(3^2 \bmod 7) \times (3^2 \bmod 7) \times (3^2 \bmod 7) \times (3^2 \bmod 7)] \bmod 7$
- ✦ $3^8 \bmod 7 = (2 \times 2 \times 2 \times 2) \bmod 7 = 16 \bmod 7 = 2$
- ✦ Note that ring Z_m (modulo arithmetic) is of central importance to modern public-key cryptography. In practice, the order of the integers involved in PKC are in the range of $[2^{160}, 2^{1024}]$. Perhaps even larger

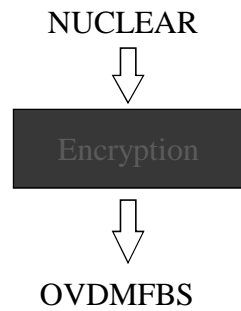
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Classic Cryptography

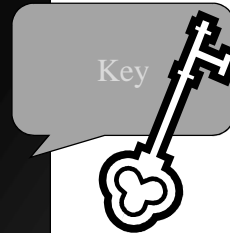
Substitution
 Transposition
 Enigma Machine
 Shift
 Affine
 Vigenere
 Block (Hill)
 Vernam (one time pad)
 Stream

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Substitution

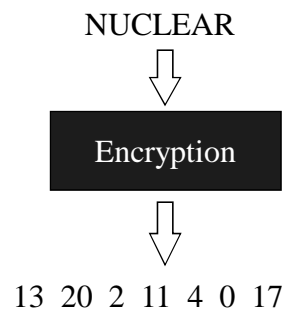


A	=>	B
B	=>	C
C	=>	D
D	=>	E
E	=>	F
.	=>	.
.	=>	.
.	=>	.
X	=>	Y
Y	=>	Z
Z	=>	A

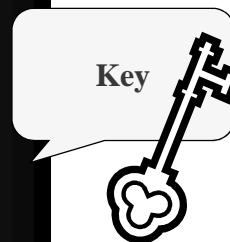


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Substitution



A	=>	0
B	=>	1
C	=>	2
D	=>	3
E	=>	4
.	=>	.
.	=>	.
.	=>	.
X	=>	23
Y	=>	24
Z	=>	25



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Advance Substitution (Random)

Key

A => D	F => I	K => N	P => S	U => G
B => A	G => J	L => O	Q => F	V => Y
C => T	H => U	M => P	R => K	W => Q
D => X	I => L	N => Z	S => V	X => E
E => H	J => R	O => M	T => W	Y => B
				Z => C



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Transposition (Permutation)

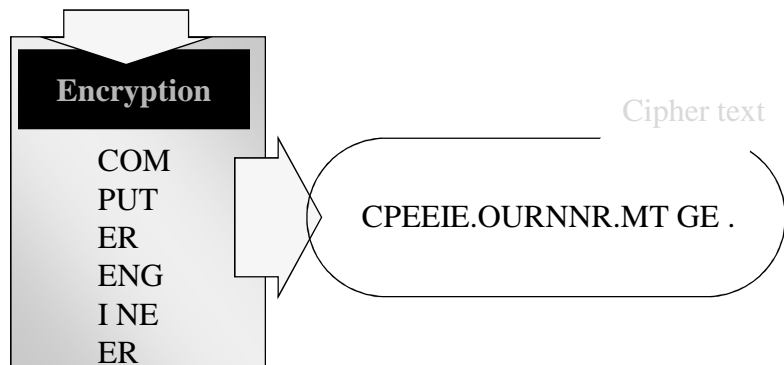
Substitution reserves places
But
Transposition reserves content



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Transposition (Permutation)

COMPUTER ENGINEER

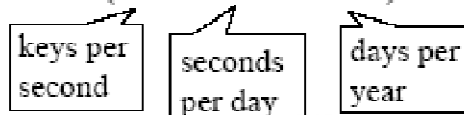


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Security

- there are $n!$ different substitutions on an alphabet with n letters
- there are $n!$ different transpositions of n letters
- $n=26$: $n!=403291461126605635584000000 = 4 \cdot 10^{26}$ keys
- trying all possibilities at 1 nanosecond per key requires....

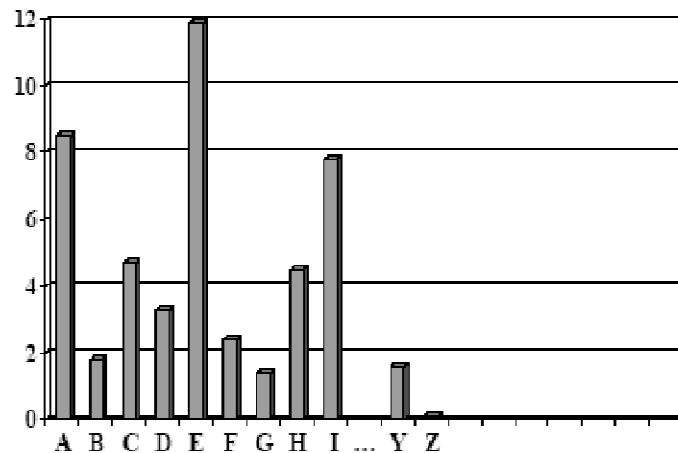
$$4 \cdot 10^{26} / (10^9 \cdot 10^6 \cdot 4 \cdot 10^2) = 10^9 \text{ years}$$



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Easy to
break simple
substitution
using
statistical
techniques

Letter distributions



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Breaking a Monoalphabetic Substitution

X ydis pq yjc xzpvpyw ya icqdepzc ayjceq xq
A tact is the ability to describe others as

yjcw qcc yjcuqcvrcq.
they see themselves.

Xzexjxu Vpsdavs
Abraham Lincoln

Character Frequency: c-10, y-8, q-7, x-6, j-5, p-5, v-4, d-3
a-3, e-3, z-3, s-2, u-2, w-2, i-1, r-1

Alphabet frequency: e t a o i n s r h l d c u m f p g w y b v k x j q

Enigma Machine

Germany- World War 1

Encryption: Keys are typed in normally

Machine output: Cipher text -
encrypted message typed on paper

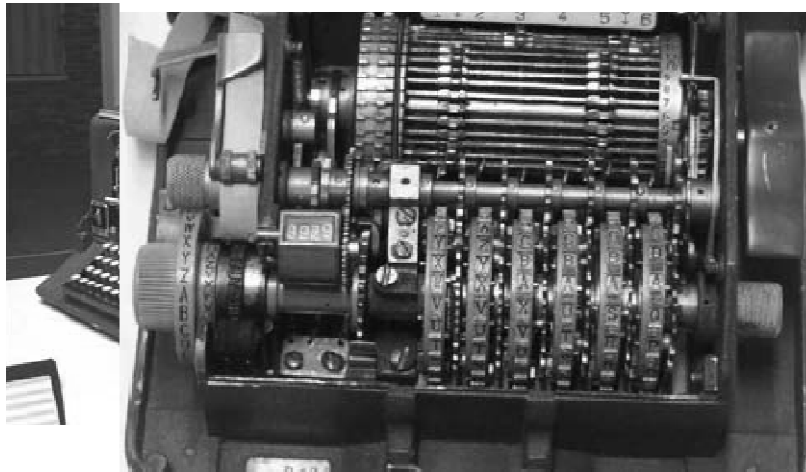
Decryption: Normal typing cipher text
- Machine output: Plain text on paper

Keys: Mechanical rotors

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Wheel Cipher

Mechanical: Hagelin C38



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Shift Cipher Analysis

✦ Alphabet letters are substituted by numbers:

A	B	C	D	E	F	G	H	I	J	K	L	M
0	1	2	3	4	5	6	7	8	9	10	11	12
N	O	P	Q	R	S	T	U	V	W	X	Y	Z
13	14	15	16	17	18	19	20	21	22	23	24	25

Ring: Z_{26} $x = \text{plaintext}$ $k = \text{key}$

– $E_k(x) = x + k \bmod 26$ (Encryption)

– $D_k(x) = x - k \bmod 26$ (Decryption)

✦ Caser Cipher: $k = 3$

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Caesar Shift

PLAINTEXT	a b c d e f g h i j k l m
CIPHERTEXT	D E F G H I J K L M N O P
PLAINTEXT	n o p q r s t u v w x y z
CIPHERTEXT	Q R S T U V W X Y Z A B C

Hello There → khoor wkhuh

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Shift Cipher Example

- ✦ Assume: key $k = 17$
- ✦ Plaintext: $X = \text{A T T A C K} = (0, 19, 19, 0, 2, 10)$.
- ✦ Ciphertext: $Y = (0+17 \bmod 26, 19+17 \bmod 26, \dots)$
- ✦ $Y = (17, 10, 10, 17, 19, 1) = \text{R K K R T B}$

Attacks on Shift Cipher

1. Exhaustive Search:

- Try all possible keys. $|K| = 26$.
- Nowadays, for moderate security, $|K| \geq 280$,
- recommended security $|K| \geq 2100$.

2. Letter frequency analysis

(Same plaintext maps to same ciphertext)

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Affine Cipher

Algorithm:

- ✦ Encryption: $E_k(x) = y = \alpha \cdot x + \beta \bmod 26$.
- ✦ Key: $k = (\alpha, \beta)$ where $\alpha, \beta \in \mathbb{Z}_{26}$ *Key Space???*
- ✦ Key space = $26 \cdot 26 = 676$ Possibilities *are they all possible?*

Example:

$k = (\alpha, \beta) = (13, 4)$

- ✦ INPUT = (8, 13, 15, 20, 19)
- ✦ $Y = (4, 17, 17, 4, 17) = \text{ERRER}$
- ✦ ALTER = (0, 11, 19, 4, 17)
- ✦ $Y = (4, 17, 17, 4, 17) = \text{ERRER}$

No one-to-one map within plaintext and ciphertext.

What went wrong?

- ✦ Decryption: $D_k(x) = x = \alpha^{-1} \cdot y + \gamma$

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Affine Cipher Analysis

Key Space:

- ✦ β can be any number in $Z_{26} \Rightarrow 26$ possibilities
- ✦ Since α^{-1} has to exist, only selected integers in Z_{26} are useful
 .e.g. $\gcd(\alpha, 26) = 1 \Rightarrow \{1, 3, 5, 7, 9, 11, 15, 17, 19, 21, 23, 25\}$
- ✦ Therefore, the key space has $12 \cdot 26 = 312$ candidates.

Attack types:

1. *Ciphertext only*: exhaustive search or frequency analysis
2. *Known plaintext*: two letters in the plaintext and corresponding ciphertext letters would be sufficient to find the key.

Example : plaintext: IF=(8, 5) and ciphertext PQ=(15, 16)

- $8 \cdot \alpha + \beta \equiv 15 \pmod{26}$
- $5 \cdot \alpha + \beta \equiv 16 \pmod{26} \quad \rightarrow \alpha = 17 \text{ and } \beta = 9$

What happens if we have only one letter of known plaintext?

3. *Chosen plaintext*: Chose A and B as the plaintext. The first character of the ciphertext will be equal to $0 \cdot \alpha + \beta = \beta$ and the second will be $\alpha + \beta$.
4. *Chosen ciphertext* : Chose A and B as the ciphertext.

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Vigenere Cipher

- ✦ *Vigenere Cipher* encrypts m alphabetic characters at a time
- ✦ each plaintext element is equivalent to m alphabetic characters
- ✦ key K is a *keyword* that associate with an alphabetic string of length m

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Example

✦ $m = 5$; $K = (2, 8, 15, 7, 20)$.

✦ $P = 4, 5, 2, 8, 11, 2, 14, 20, 1, 2, 4, 5, 16$

✦ Encryption:

4	5	2	8	11	2	14	20	1	2	3	4	5	16
2	8	15	7	20	2	8	15	7	20	2	8	15	7
6	13	17	15	31	4	22	9	8	22	5	12	20	23

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Vigenere Cipher Secrecy

- ✦ number of possible keywords of length $m \rightarrow 26^m$
- ✦ if $m = 5$, then the keyspace has size exceeding 1.1×10^7 .
- ✦ This is already large enough to preclude exhaustive key search by hand (but not by computer).
- ✦ having keyword length m , an alphabetic character can be mapped to one of m possible alphabetic characters (assuming that the keyword contains m distinct characters).
- ✦ Such a cryptosystem is called *polyalphabetic*.
- ✦ In general, cryptanalysis is more difficult for polyalphabetic than for monoalphabetic cryptosystems.

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Vigenere Cipher Attack

- ✦ observe two identical segments in Ciphertext each of length at least three, then there is a good chance that they do correspond to identical segments of plaintext.

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Block ciphers

Substitution ciphers: changing one letter in the plaintext changes exactly one letter in the ciphertext.

- ✦ This greatly facilitates finding the key using frequency analysis.

Block ciphers: prevents this by encrypting a block of letters simultaneously.

- ✦ Many of the modern (symmetric) cryptosystems are block ciphers.
- ✦ DES operates on 64 bits of blocks
- ✦ AES uses blocks of 128 bits (192 and 256 are also possible).

Example: Hill Cipher (1929)

- ✦ The key is an $n \times n$ matrix whose entries are integers in \mathbb{Z}_{26} .

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Block cipher: Hill cipher

✦ Encryption: vector-matrix multiplication

✦ **Example:** Let $n=3$, key matrix ' M ' be $M = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 11 & 9 & 8 \end{pmatrix}$
assume the plaintext is $ABC=(0,1,2)$

$$(0,1,2) \times \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 11 & 9 & 8 \end{pmatrix} \equiv (26,23,22) \bmod 26 = (0,23,22) \Rightarrow AXW(\text{ciphertext})$$

Decryption:

$$(0,23,22) \times \begin{pmatrix} 22 & 5 & 1 \\ 6 & 17 & 24 \\ 15 & 13 & 1 \end{pmatrix} \equiv (468,677,574) \bmod 26 = (0,1,2) \Rightarrow ABC(\text{plain-text})$$

Hill Cipher

✦ If we change one letter in the plaintext, all the letters of the ciphertext will be affected.

Example:

✦ Let the plaintext be ABB instead of ABC then the ciphertext is

$$(0,1,1) \times \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 11 & 9 & 8 \end{pmatrix} \equiv (15,14,14) \bmod 26 = (15,14,14) \Rightarrow POO(\text{ciphertext})$$

Another Example

➤ Use Key:

$$M = \begin{pmatrix} 6 & 24 & 1 \\ 13 & 16 & 10 \\ 20 & 17 & 15 \end{pmatrix}$$

➤ Decryption Key:

$$N = \begin{pmatrix} 8 & 5 & 10 \\ 21 & 8 & 21 \\ 21 & 12 & 8 \end{pmatrix}$$

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Hill Cipher Attack

➤ Ciphertext:

- Hill Cipher is more difficult to break with a ciphertext-only attack.

➤ Plaintext + Ciphertext:

1. Opponent has determined the value of m
2. Compute the key

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Properties of Good Cryptosystems

- ✦ **Diffusion:** one character change in the plaintext should effect as many ciphertext characters as possible.
- ✦ **Confusion:** The key should not relate to the ciphertext in a simple way.

Shannon (1949)

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One-Time Pad (Vernam Cipher)

- ✦ Vernam in 1918, proposed the one-time pad, which is a provably secure cryptosystem.
- ✦ Messages are represented as a binary string (a sequence of 0's and 1's using a coding mechanism such as ASCII coding.)
- ✦ The key is a truly random sequence of 0's and 1's of the same length as the message.
- ✦ The encryption is done by adding the key to the message modulo 2, bit by bit as *exclusive OR*, \oplus (XOR).

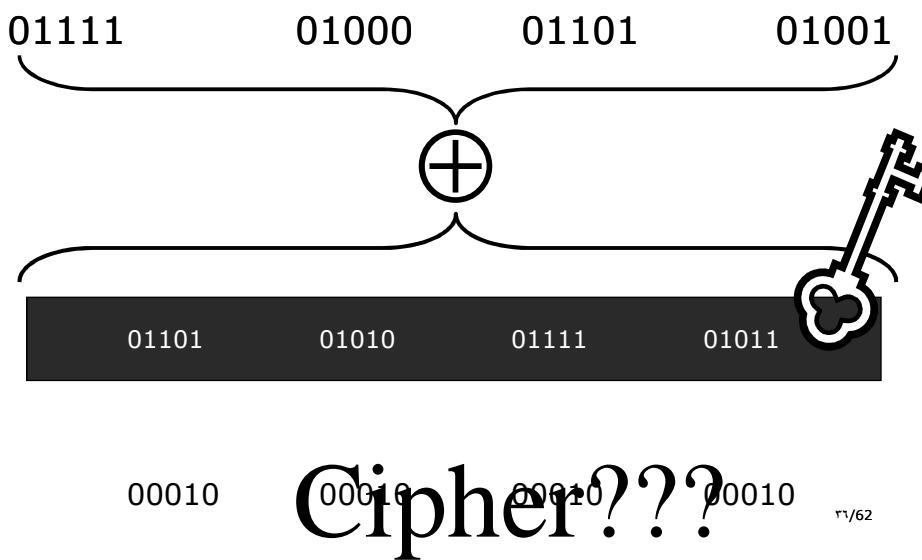
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One-time pad

- ✦ Secret-key encryption scheme (symmetric)
 - Encrypt plaintext by XOR with sequence of bits
 - Decrypt ciphertext by XOR with same bit sequence
- ✦ Scheme for pad of length n
 - Set P of plaintexts: all n -bit sequences
 - Set C of ciphertexts: all n -bit sequences
 - Set K of keys: all n -bit sequences
 - Encryption and decryption functions
 - $\text{encrypt}(\text{key}, \text{text}) = \text{key} \oplus \text{text}$ (bit-by-bit)
 - $\text{decrypt}(\text{key}, \text{text}) = \text{key} \oplus \text{text}$ (bit-by-bit)

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Unconditional Secure



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Vernam scheme: perfect secrecy

- general: $C = (P + K) \bmod 26$; $P = (C - K) \bmod 26$
 - with $C, P, K \in [0, 25]$; $A=0, B=1, \dots, Z=25$
- consider ciphertext $C = \text{XHGRQ}$
 - with key AAAAA $P = \text{XHGRQ}$
 - with key VAYEK $P = \text{CHINA}$
 - with key EZANZ $P = \text{TIGER}$
 - ...
 - with key ZZZZZ $P = \text{YIHSR}$
- conclusion: for every 5-character plaintext there is a 5-character key which maps the ciphertext to that plaintext

Evaluation of one-time pad

Advantages

- Easy to compute encrypt, decrypt from key, text
- As hard to break as possible
 - ✦ This is an information-theoretically secure cipher
 - ✦ Given ciphertext, all possible plaintexts are equally likely, assuming that key is chosen randomly

Disadvantage

- Key is as long as the plaintext
 - ✦ How does sender get key to receiver securely?

Idea for stream cipher: use pseudo-random generators for key...

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Randomness & Pseudo-randomness

Randomness: Closely related to *unpredictability*

Pseudo-randomness : PR sequences appears random to a computationally bounded adversary

Cryptosystems need random unpredictable numbers for

- ✦ One-time pad
- ✦ Secret key for DES, AES, etc.
- ✦ Primes p, q for RSA
- ✦ Private key for ECC
- ✦ Challenges used in challenge based identification systems

True random number generation (RNG)

Requires a naturally occurring source of randomness
(randomness exists in the nature)

- ✦ Hardware based random number generators (RNG) exploit the randomness which occurs in some physical phenomena
 - Elapsed time between emission of particles during radioactive decay
 - Thermal noise from a semiconductor diode or resistor
 - Frequency instability of a free running oscillator
 - The amount which a metal insulator semiconductor capacitor is charged during a fixed period of time.
- ✦ The first two are subject to observation and manipulation by adversaries.

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Software base RNG

1. The system clock
 2. Elapsed time between keystrokes or mouse movement
 3. Content of input/output buffer
 4. User input
 5. OS values such as system load and network statistics.
- ✦ All of them are subject to observation and manipulation.
 - ✦ Individually these sources are very “weak”.
 - ✦ The randomness can be increased by combining the outputs of these sources using a complex mixing function (e.g. hashing the concatenation of the output bits).
 - ✦ Still, not quite secure!

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Pseudorandom number generation

- ✦ A pseudorandom number generator (PRNG) is a deterministic algorithm, which, given a truly random binary sequence of length k (*random seed*), outputs a binary sequence of length $l \gg k$ which “appears” to be random.
- ✦ The output of a PRNG is not random. However, it is impractical (improbable) for anyone (adversary) to distinguish a pseudorandom sequence from a truly random sequence of the same length.
- ✦ No practical test to check if a sequence is truly random.
- ✦ Thus, we can’t define exactly what the pseudo randomness.
- ✦ Golomb’s postulates was one of the first attempt to establish necessary conditions for a periodic sequence to look random. It has only historical importance nowadays.
- ✦ However, more recent attempts may not offer a more thorough conditions.

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Statistical Tests for Pseudo-randomness

1. Frequency test (mono bit test):
 - ✦ # of 1s and 0s must be approximately the same
2. Poker test
 - ✦ A sequence is divided into k non-overlapping segments of length m .
 - ✦ This test determines if the segments of length m each appear approximately the same number of times.
3. Runs Test
 - ✦ Determines if the # of runs of various lengths is similar to those of truly random sequences
4. Long run test
 - ✦ The long run test is passed if there are no runs of length 34 or more.

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Stream Ciphers

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Basic Idea

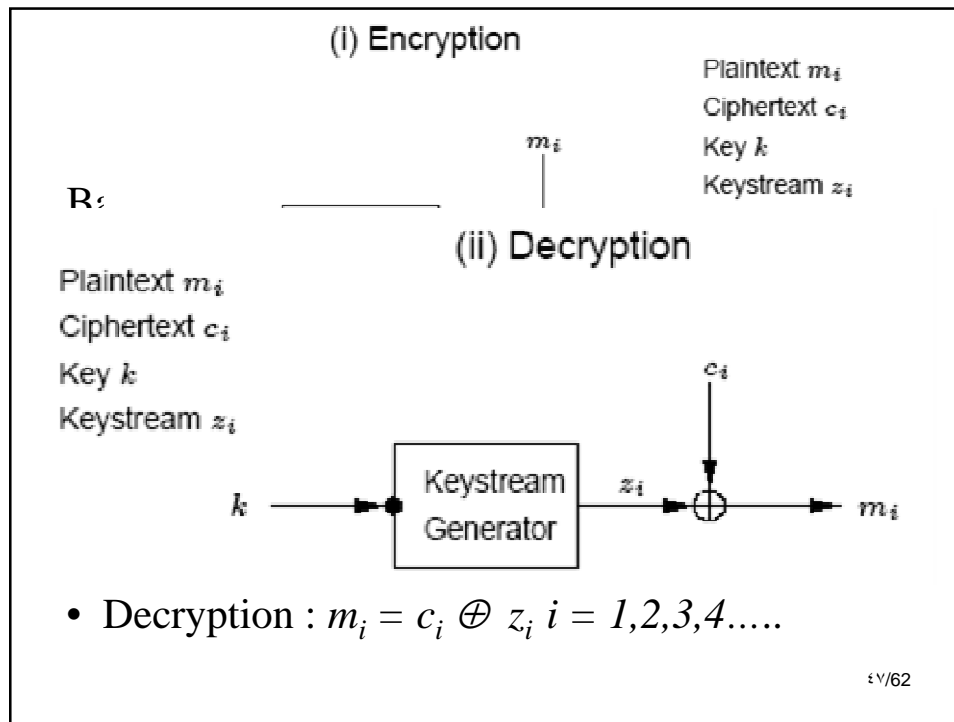
- Block ciphers: $y = y_1 y_2 y_3 = E_K(x_1) E_K(x_2) E_K(x_3)$
- Stream cipher: $y = y_1 y_2 y_3 = E_{z_1}(x_1) E_{z_2}(x_2) E_{z_3}(x_3)$
- Stream cipher Key: $z_i = f(K, x_1, x_2)$
- block cipher can be a special case of a stream cipher where the key-stream is constant

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Binary Stream

- Stream ciphers are often described in terms of binary alphabets
- the encryption and decryption operation are just addition modulo 2
- exclusive-or operation: XOR ‘ \oplus ’
- implemented very efficiently in hardware

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Stream Cipher

- **Drawback :**
 - Key-stream should be as long as plain-text.
 - Key distribution & Management difficult.
- **Solution :**
 - Stream Ciphers (in which key-stream is generated in pseudo-random fashion from relatively short *secret key*.)

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Stream ciphers

- **Randomness :**
 - Closely related to *unpredictability*.
- **Pseudo-randomness :**
 - PR sequences appears random to a computationally bounded adversary.
 - Stream Ciphers can be modeled as Finite-state machine.

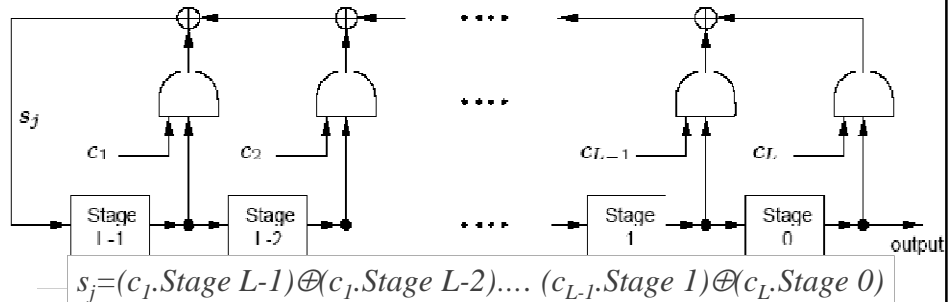
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Linear Feedback Shift Register (LFSR)

- Well-suited for hardware implementation
- Very low implementation costs
- Produce sequences:
 - having large periods
 - having good statistical properties
 - readily analyzed using algebraic techniques
- But, the output sequences of LFSRs are easily predictable.

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Linear Feedback Shift Register (LFSR)



Connection Polynomial: $C(x) =$

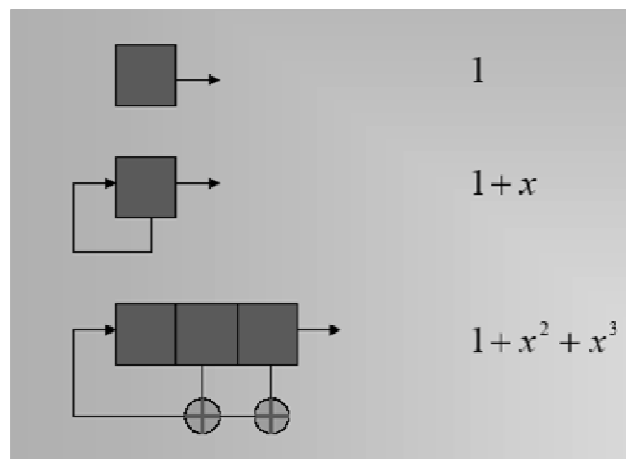
$$1 + c_1x + c_2x^2 + c_3x^3 + \dots + c_Lx^L$$

If $C(x)$ is chosen carefully the output of LFSR can have maximum period of $2^L - 1$

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LFSR

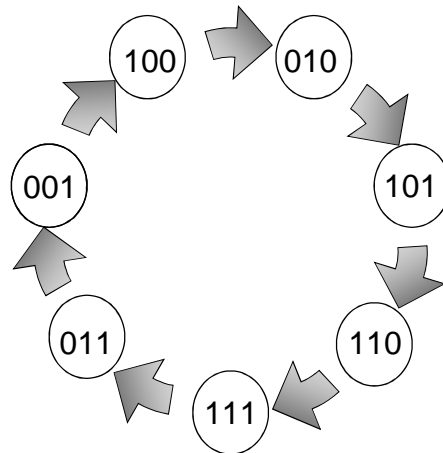
Connection Polynomial Generation



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LFSR

Example: $C(x) = x^3 + x^2 + 1$



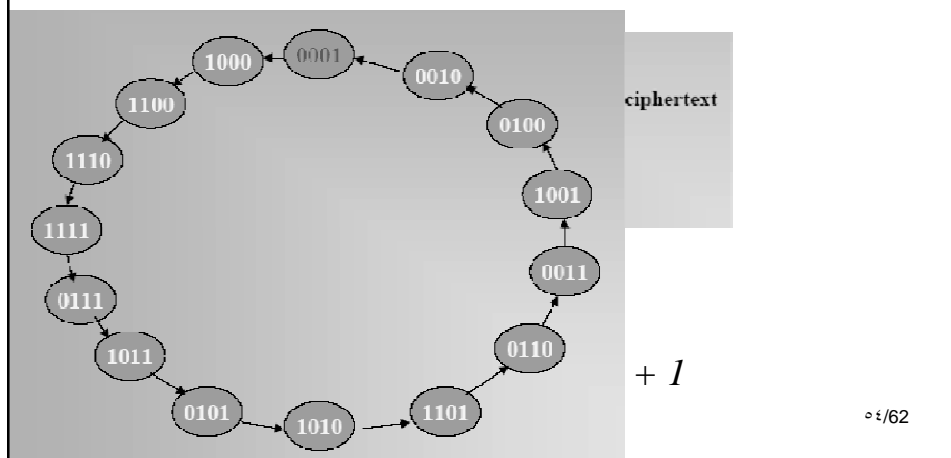
Compare with: $C(x) = x^3 + x + 1$

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LFSR Example

when initial state is (0001)

LSFR Output: 100011110101100 100011110101100 ...



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LFSR

- *LFSR* have good statistical properties.
- However, they may be predictable

Caveat/Warning:

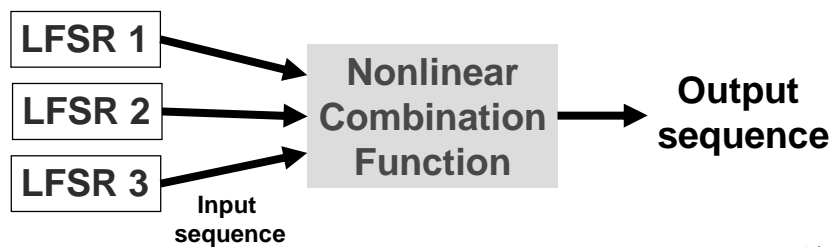
- Mathematical proofs of security of such generators are not known.
- They are deemed to be computationally secure after having withstood sufficient public scrutiny and inspection.

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Nonlinear Combination Generator

Combiner function must be

- Balanced
- highly nonlinear
- carefully selected → no dependence between any subset of LFSR sequences and the output sequence



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Example: Geffe generator

$$F(x_1, x_2, x_3) = x_1 x_2 \oplus x_2 x_3 \oplus x_3$$

- inspect the truth table of the combiner function to gain more insight about the security of Geffe generator.
- The combiner function is balanced
- However, the correlation of z to
 - x_1 is $P(z=x_1) = \frac{3}{4}$
 - x_2 is $P(z=x_2) = \frac{1}{2}$
 - x_3 is $P(z=x_3) = \frac{3}{4}$

x_1	x_2	x_3	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

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Geffe Generator Example Study

- LFSR#1: $1+x+x^4$. Initial key1: 1000
- LFSR#2: $1+x+x^3$. Initial key2: 110
- LFSR#3: $1+x^2+x^5$. Initial key3: 10101
- Key sequence 1 (x_1): 100011110101100
- Key sequence 2 (x_2): 010011101001110
- Key sequence 3 (x_3): 101011101100011
- Output sequence (z): 101011100101101
- Exhaustive search: $15 \times 7 \times 31 = 3255$

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Correlation Attack

- If we have n LFSRs, the key space of the non-linear combination generator is the product of their non-repetitive shortest sequence terms.

Exhaustive search = Brute force attack: $15 \times 7 \times 31 = 3255$ trial

- However, if there is correlation between the output sequence and each input sequence then the *effective* key length can be reduced to the summation of their non-repetitive shortest sequence terms.

Correlation attack: $15 + 7 + 31 = 53$ trial

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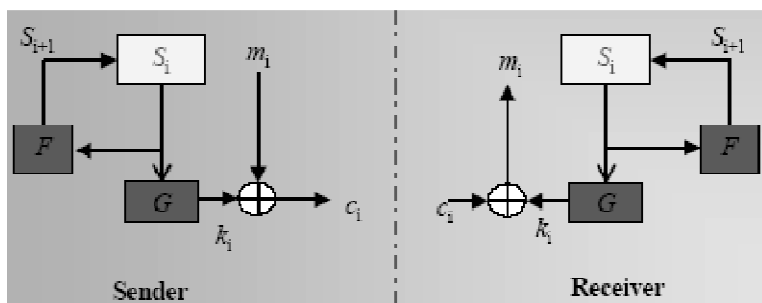
Correlation Attack

z	1	0	1	0	1	1	1	0	0	1	0	1	1	0	1	
$x^{(1)}_1$	1	1	1	0	1	0	1	1	0	0	1	0	0	0	1	8/15
$x^{(2)}_1$	1	1	0	1	0	1	1	0	0	1	0	0	0	1	1	8/15
$x^{(3)}_1$	1	0	1	0	1	1	0	0	1	0	0	0	1	1	1	10/15
$x^{(4)}_1$	0	1	0	1	1	0	0	1	0	0	0	1	1	1	1	6/15
$x^{(5)}_1$	1	0	1	1	0	0	1	0	0	0	1	1	1	1	0	8/15
$x^{(6)}_1$	0	1	1	0	0	1	0	0	0	1	1	1	1	0	1	10/15
$x^{(7)}_1$	1	1	0	0	1	0	0	0	1	1	1	1	0	1	0	6/15
$x^{(8)}_1$	1	0	0	1	0	0	0	1	1	1	1	0	1	0	1	6/15
$x^{(9)}_1$	0	0	1	0	0	0	1	1	1	1	0	1	0	1	1	8/15
$x^{(10)}_1$	0	1	0	0	0	1	1	1	1	0	1	0	1	1	0	4/15
$x^{(11)}_1$	1	0	0	0	1	1	1	1	0	1	0	1	1	0	0	12/15
$x^{(12)}_1$	0	0	0	1	1	1	1	0	1	0	1	1	0	0	1	7/15

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Synchronous Stream Ciphers

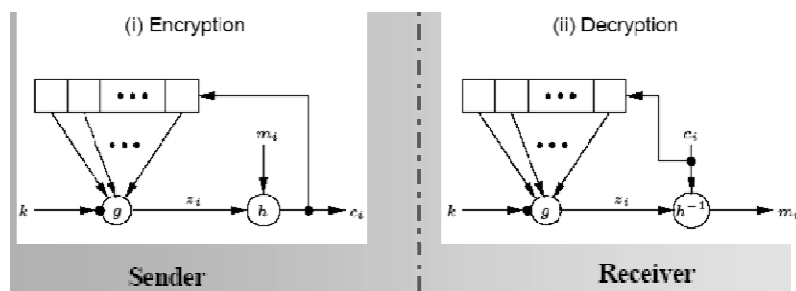
- Key-stream is independent of plain and cipher-text.
- Both sender & receiver must be synchronized.
- Resynchronization can be needed.
- Active attacks can easily be detected. (insertion, deletion, replay)
- No Error Propagation.



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Self-Synchronizing (Asynchronous) Stream Ciphers

- key stream generated as function of fixed number of previous ciphertext bits
- Active attacks cannot be detected.
- At most t bits later than synchronization is lost, it resynchronizes itself
- Limited error propagation (up to t bits).



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SEAL (just an idea)

- SEAL (Software-optimized Encryption Algorithm) is a binary additive stream cipher (proposed 1993)
- specifically designed for efficient software implementation for 32-bit processors
- it has not yet received much scrutiny from the cryptographic community

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